

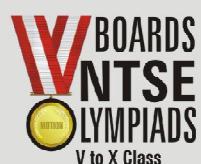
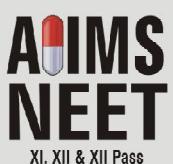
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JEE  
MAIN  
JAN  
2020

## PAPER WITH SOLUTION

9<sup>th</sup> January 2020 \_ SHIFT - 1

### MATHEMATICS



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**Sol.**

\_

$$=t^4 + t^3 - 4t^2 + t + 1 = 0$$

$$= \left( t^2 + \frac{1}{t^2} \right) + \left( t + \frac{1}{t} \right) - 4 = 0$$

$$= \left( t + \frac{1}{t} \right)^2 + \left( t + \frac{1}{t} \right) - 6 = 0$$

$$\Rightarrow u^2 + u - 6 = 0$$

$$\Rightarrow (u+3)(u-2)=0$$

$$t + \frac{1}{t} - 2 = 0 \quad ; \quad t + \frac{1}{t} + 3 = 0 \text{ (Not possible)}$$

$$\Rightarrow t^2 - 2t + 1 = 0$$

$$\Rightarrow t = 1$$

$$\Rightarrow e^x = 1$$

$$\Rightarrow x = 0$$

- ## **2. Negation of the statement :**

$\sqrt{5}$  is an integer or 5 is irrational is :

- (1)  $\sqrt{5}$  is an integer and 5 is irrational.
  - (2)  $\sqrt{5}$  is not an integer and 5 is not irrational.
  - (3)  $\sqrt{5}$  is not an integer or 5 is not irrational.
  - (4)  $\sqrt{5}$  is irrational or 5 is an integer.

कथन,  $\sqrt{5}$  एक पूर्णांक है या अपरिमेय है' का निषेधन है :

- (1)  $\sqrt{5}$  एक पूर्णांक नहीं है या 5 अपरिमेय नहीं है।

(2)  $\sqrt{5}$  एक पूर्णांक नहीं है या 5 अपरिमेय नहीं है।

(3)  $\sqrt{5}$  एक पूर्णांक है और 5 अपरिमेय है।

(4)  $\sqrt{5}$  अपरिमेय है या 5 एक पूर्णांक है।

Sol. 2

$$\sim(p \vee q) = \sim p \wedge \sim q$$

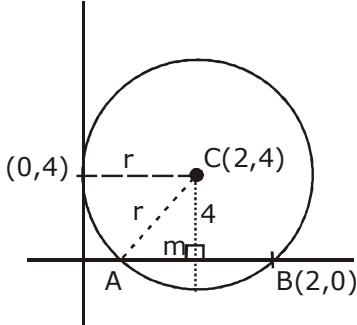


5. A circle touches the y-axis at the point (0,4) and passes through the point (2,0). Which of the following lines is not a tangent to this circle?

एक वृत्त y-अक्ष को बिन्दु (0, 4) पर स्पर्श करता है तथा बिन्दु (2, 0) से होकर जाता है। निम्न में से कौन सी रेखा इस वृत्त की स्पर्श रेखा नहीं है?

- (1)  $3x - 4y - 24 = 0$     (2)  $4x - 3y + 17 = 0$     (3)  $3x + 4y - 6 = 0$     (4)  $4x + 3y - 8 = 0$

**Sol. 4**



$$x^2 + (y - 4)^2 + \lambda x = 0$$

Passes through (2, 0)

$$4 + 16 + 2\lambda = 0$$

$$\lambda = -10$$

$$x^2 + y^2 - 8x + 16 - 10y = 0$$

$$C(5, 4), \quad r = \sqrt{25 + 16 + 16} = 5$$

$$\text{Option (1)} \quad p = \frac{|15 - 16 - 24|}{5} = 5$$

$$\text{Option (2)} \quad p = \frac{|20 - 12 + 17|}{5} = 5$$

$$\text{Option (3)} \quad p = \frac{|15 + 16 - 6|}{5} = 5$$

$$\text{Option (4)} \quad p = \frac{|20 + 12 - 8|}{5} \neq 5$$

6. Let z be a complex number such that

$$\left| \frac{z-i}{z+2i} \right| = 1 \text{ and } |z| = \frac{5}{2}. \text{ Then the value of } |z+3i| \text{ is :}$$

माना z एक ऐसी सम्मिश्र संख्या है, कि  $\left| \frac{z-i}{z+2i} \right| = 1$  है तथा  $|z| = \frac{5}{2}$  है, तो  $|z+3i|$  का मान है :

- (1)  $\frac{7}{2}$     (2)  $\frac{15}{4}$     (3)  $2\sqrt{3}$     (4)  $\sqrt{10}$

**Sol. 1**

$$\left| \frac{z-i}{z+2i} \right| = 1 \quad , |z| = \frac{5}{2} \Rightarrow x^2 + (y-1)^2 = x^2 + (y+2)^2$$

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$$\Rightarrow y = -\frac{1}{2} \quad \dots(1) \quad \Rightarrow |z| = \frac{5}{2}$$

$$x^2 + y^2 = \frac{25}{4}$$

from eq.(1)

$$\Rightarrow x = \pm \sqrt{6}$$

$$z = \sqrt{6} - \frac{i}{2} \text{ or } -\sqrt{6} - \frac{i}{2}$$

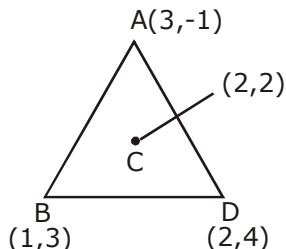
$$|z+3i| = \left| \sqrt{6} - \frac{i}{2} + 3i \right| \text{ or } \left| -\sqrt{6} - \frac{i}{2} + 3i \right| \Rightarrow \sqrt{6 + \frac{25}{4}} = \sqrt{\frac{49}{4}} = \frac{7}{2}$$

7. Let C be the centroid of the triangle with vertices (3, -1), (1, 3) and (2, 4). Let P be the point of intersection of the lines  $x + 3y - 1 = 0$  and  $3x - y + 1 = 0$ . Then the line passing through the points C and P also passes through the point.

माना शीर्षों (3, -1), (1, 3) तथा (2, 4) वाले त्रिभुज का केन्द्रक C है। माना रेखाओं  $x + 3y - 1 = 0$  तथा  $3x - y + 1 = 0$  का प्रतिच्छेदन बिन्दु P है, तो बिन्दुओं C तथा P से गुजरने वाली रेखा, निम्न में से किस बिन्दु से भी गुजरती है?

- (1) (-9, -7)      (2) (9, 7)      (3) (7, 6)      (4) (-9, -6)

Sol. 4



$$P: x + 3y - 1 = 0 \dots(1)$$

$$3x - y + 1 = 0 \dots(2)$$

On solving eq.(1) and (2)

$$x = -\frac{1}{5}, y = \frac{2}{5}$$

eq.of line CP :

$$= y - 2 = \left( \frac{\frac{2}{5} - 2}{-\frac{1}{5} - 2} \right) (x - 2)$$

$$\Rightarrow 8x - 11y + 6 = 0$$

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**8.** If the number of five digit numbers with distinct digits and 2 at the 10<sup>th</sup> place is 336k, then k is equal to :

यदि विभिन्न अंकों वाली पांच अंकों की संख्याओं, जिनका दहाई का अंक 2 है, की संख्या  $336k$  है, तो  $k$  बराबर है :



**Sol.**

**3**      8      7      1      6  
↑      ↑      ↑      ↑      ↑

2

$$8 \times 8 \times 7 \times 6 = 336k$$

k = 8

- 9.** The integral  $\int \frac{dx}{(x+4)^{8/7}(x-3)^{6/7}}$  is equal to : (where C is a constant of integration)

$$\text{समाकल } \int \frac{dx}{(x+4)^{8/7}(x-3)^{6/7}} \text{ बराबर है : (जहाँ C एक समाकलन अचर है)}$$

- $$(1) \frac{1}{2} \left( \frac{x-3}{x+4} \right)^{3/7} + C \quad (2) \left( \frac{x-3}{x+4} \right)^{1/7} + C \quad (3) - \left( \frac{x-3}{x+4} \right)^{-1/7} + C \quad (4) - \frac{1}{13} \left( \frac{x-3}{x+4} \right)^{-13/7} + C$$

Sol. 2

$$\int \frac{dx}{(x+4)^{\frac{8}{7}}(x-3)^{\frac{6}{7}}}$$

$$\int \frac{dx}{(x+4)^2 \left(\frac{x-3}{x+4}\right)^{6/7}}$$

$$\text{Put } \frac{x-3}{x+4} = t^7$$

$$\left( \frac{(x+4)-(x-3)}{(x+4)^2} \right) dx = 7t^6 dt$$

$$\frac{7}{(x+4)^2} dx = 7t^6 dt$$

$$\int \frac{t^6}{t^6} dt = \left( \frac{x-3}{x+4} \right)^{\frac{1}{7}} + C$$

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10. If  $f(x) = \begin{cases} \frac{\sin(a+2)x + \sin x}{x}; & x < 0 \\ b & ; x = 0 \\ \frac{(x+3x^2)^{1/3} - x^{1/3}}{x^{4/3}}; & x > 0 \end{cases}$

is continuous at  $x = 0$ , then  $a + 2b$  is equal to :

यदि  $f(x) = \begin{cases} \frac{\sin(a+2)x + \sin x}{x}; & x < 0 \\ b & ; x = 0 \\ \frac{(x+3x^2)^{1/3} - x^{1/3}}{x^{4/3}}; & x > 0 \end{cases}$

$x = 0$  पर संतत है, तो  $a + 2b$  का मान है :

(1) 1

(2) 0

(3) -1

(4) -2

**Sol.** 2

$$f(0^-) = \lim_{h \rightarrow 0} \frac{\sin(a+2)h + \sin h}{h}$$

$$= \lim_{h \rightarrow 0} \frac{2 \sin\left(\frac{(a+3)}{2}\right)h \cos\left(\frac{a+1}{2}\right)h}{\frac{(a+3)}{2} \times h} \times \frac{(a+3)}{2} = a + 3$$

$$= f(0^+) = \lim_{h \rightarrow 0} \frac{(h+3h^2)^{1/3} - h^{1/3}}{h^{4/3}}$$

$$= f(0^+) = \lim_{h \rightarrow 0} \frac{1+h-1}{h} = 1$$

$$= a + 3 = 1 = b$$

$$a = -2, b = 1$$

$$a + 2b = 0$$

11. The product

$$2^{\frac{1}{4}} \cdot 4^{\frac{1}{16}} \cdot 8^{\frac{1}{48}} \cdot 16^{\frac{1}{128}} \dots \text{to } \infty \text{ is equal to :}$$

$$\text{गुणनफल } 2^{\frac{1}{4}} \cdot 4^{\frac{1}{16}} \cdot 8^{\frac{1}{48}} \cdot 16^{\frac{1}{128}} \dots \infty \text{ तक बराबर है :}$$

(1)  $2^{\frac{1}{4}}$

(2)  $2^{\frac{1}{2}}$

(3) 2

(4) 1

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**Sol.**    **2**  
 $= 2^{1/4} \cdot 2^{1/8} \cdot 2^{1/16} \cdot 2^{1/32} \dots$

$$= 2^{\frac{1}{4} + \frac{1}{8} + \frac{1}{16} + \frac{1}{32} + \dots} = 2^{\frac{\frac{1}{4}}{1 - \frac{1}{2}}} = 2^{1/2}$$

- 12.** If  $f'(x) = \tan^{-1}(\sec x + \tan x)$ ,  $-\frac{\pi}{2} < x < \frac{\pi}{2}$ , and  $f(0) = 0$ , then  $f(1)$  is equal to :

यदि  $f'(x) = \tan^{-1}(\sec x + \tan x)$ ,  $-\frac{\pi}{2} < x < \frac{\pi}{2}$  है तथा  $f(0) = 0$  है, तो  $f(1)$  का मान है :

- $$(1) \frac{\pi+2}{4} \quad (2) \frac{1}{4} \quad (3) \frac{\pi+1}{4} \quad (4) \frac{\pi-1}{4}$$

Sol. 3

$$= f'(x) = \tan^{-1} \left[ \frac{1 + \sin x}{\cos x} \right]$$

$$= f'(x) = \tan^{-1} \left[ \tan \left( \frac{\pi}{4} + \frac{x}{2} \right) \right]$$

$$= f'(x) = \frac{\pi}{4} + \frac{x}{2}, \quad \begin{cases} -\frac{\pi}{4} < \frac{x}{2} < \frac{\pi}{4} \\ 0 < \frac{x}{2} + \frac{\pi}{4} < \frac{\pi}{2} \end{cases}$$

$$= f(x) = \frac{\pi x}{4} + \frac{x^2}{4} + C$$

$$f(0) = 0 \quad \Rightarrow \quad C = 0$$

$$= f(x) = \frac{\pi x}{4} + \frac{x^2}{4} \quad = f(1) = \frac{\pi + 1}{4}$$

- 13.** Let  $f$  be any function continuous on  $[a, b]$  and twice differentiable on  $(a, b)$ . If for all  $x \in (a, b)$ ,  $f'(x) > 0$

and  $f''(x) < 0$ , then for any  $c \in (a, b)$ ,  $\frac{f(c) - f(a)}{f(b) - f(c)}$  is greater than :

माना  $f$  कोई फलन है जोकि  $[a, b]$  में संतत तथा  $(a, b)$  में दो बार अवकलनीय है। यदि सभी  $x \in (a, b)$  के लिए  $f'(x) > 0$

तथा  $f'(x) < 0$  है, तो किसी भी  $c \in (a, b)$  के लिए  $\frac{f(c) - f(a)}{f(b) - f(c)}$  निम्न में से किससे बड़ा है ?

- $$(1) \frac{c-a}{b-c} \quad (2) \frac{b-c}{c-a} \quad (3) \frac{b+c}{b-a} \quad (4) 1$$

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$$= \frac{60 - 30}{10} = 3 = \mu$$

$$\text{Variance} = \frac{\sum x_i^2}{n} - (\bar{x})^2$$

$$= \frac{(x_1 - 3)^2 + \dots + (x_{10} - 3)^2}{10} - 3^2$$

$$= \frac{390 + 90 - 6 \times 60}{10} - 3^2 = 3$$

15. A spherical iron ball of 10 cm radius is coated with a layer of ice of uniform thickness that melts at a rate of  $50 \text{ cm}^3/\text{min}$ . When the thickness of ice is 5 cm, then the rate (in  $\text{cm}/\text{min}$ ) at which of the thickness of ice decreases, is :

एक 10 cm त्रिज्या वाली गोलाकार लोहे की गेंद को बर्फ की एक समान मोटाई वाली परत से लेप किया गया है, जो कि  $50 \text{ cm}^3/\text{min}$  की दर से पिघलती है। जब बर्फ की परत की मोटाई 5 cm है, उस समय बर्फ की मोटाई के घटने की दर ( $\text{cm}/\text{min}$  में), है :

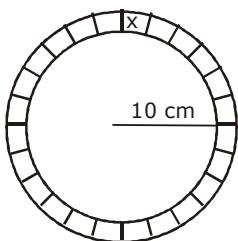
(1)  $\frac{1}{18\pi}$

(2)  $\frac{5}{6\pi}$

(3)  $\frac{1}{36\pi}$

(4)  $\frac{1}{54\pi}$

**Sol. 1**



$$V = \frac{4}{3}\pi(r+x)^3$$

$$V = \frac{4}{3}\pi(10+x)^3$$

$$\frac{dV}{dt} = 4\pi(10+x)^2 \frac{dx}{dt}$$

$$50 = 4\pi(10+x)^2 \frac{dx}{dt}$$

$$\frac{dx}{dt} = \frac{50}{4\pi(15)^2} = \frac{50}{4\pi \times 15 \times 15} = \frac{1}{18\pi} \text{ cm/min}$$

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- 16.** If the matrices  $A = \begin{bmatrix} 1 & 1 & 2 \\ 1 & 3 & 4 \\ 1 & -1 & 3 \end{bmatrix}$ ,  $B = \text{adj } A$  and  $C = 3A$ , then  $\frac{|\text{adj } B|}{|C|}$  is equal to :

यदि आव्यूह  $A = \begin{bmatrix} 1 & 1 & 2 \\ 1 & 3 & 4 \\ 1 & -1 & 3 \end{bmatrix}$ ,  $B = \text{adj } A$  तथा  $C = 3A$  हैं, तो  $\frac{|\text{adj } B|}{|C|}$  का मान है :

- Sol.** (1) 8 (2) 2 (3) 16 (4) 72

$$\frac{|\text{adj}(\text{adj}A)|}{|c|} = \frac{|A|^{(n-1)^2}}{|c|}$$

$$d = \frac{(6)^{(3-1)^2}}{3^3 |A|} = \frac{6^4}{6 \times 27} = 8$$

- 17.** If for all real triplets  $(a, b, c)$ ,  $f(x) = a + bx + cx^2$ ; then  $\int_0^1 f(x)dx$  is equal to :

यदि सभी वास्तविक त्रिकों  $(a, b, c)$  के लिए,  $f(x) = a + bx + cx^2$  है, तो  $\int_a^b f(x)dx$  बराबर है :

- $$(1) \quad 2\left\{3f(1)+2f\left(\frac{1}{2}\right)\right\} \quad (2) \quad \frac{1}{2}\left\{f(1)+3f\left(\frac{1}{2}\right)\right\} \quad (3) \quad \frac{1}{3}\left\{f(0)+f\left(\frac{1}{2}\right)\right\} \quad (4) \quad \frac{1}{6}\left\{f(0)+f(1)+4f\left(\frac{1}{2}\right)\right\}$$

Sol. 4

$$\Rightarrow \int_0^1 (a + bx + cx^2) dx$$

$$\left( ax + \frac{bx^2}{2} + \frac{x^3}{3} \right)_0^1$$

$$a + \frac{b}{2} + \frac{c}{3} \Rightarrow \frac{6a + 3b + 2c}{6}$$

$$f\left(\frac{1}{2}\right) = a + \frac{b}{2} + \frac{c}{4}$$

$$f(0)=0$$

$$(A) 2\{3(a+b+c) + 2a + b + c/2\} \\ = 2\{5a + 4b + 7c/2\}$$

$$(B) \frac{1}{2} \left\{ a + b + c + 3a + \frac{3b}{2} + \frac{3c}{4} \right\}$$

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**Fees - ₹ 0**  
score above 240

$$\frac{1}{2} \left\{ 4a + \frac{5b}{2} + \frac{7c}{4} \right\}$$

$$(D) \frac{1}{6} \left[ a + a + b + c + 4 \left( a + \frac{b}{2} + \frac{c}{4} \right) \right]$$

$$\frac{1}{6}[6a + 3b + 2c]$$

- 18.** If  $e_1$  and  $e_2$  are the eccentricities of the ellipse,  $\frac{x^2}{18} + \frac{y^2}{4} = 1$  and the hyperbola,  $\frac{x^2}{9} - \frac{y^2}{4} = 1$  respectively and  $(e_1, e_2)$  is a point on the ellipse,  $15x^2 + 3y^2 = k$ , then  $k$  is equal to :

यदि  $e_1$  तथा  $e_2$  क्रमशः दीर्घवत्  $\frac{x^2}{18} + \frac{y^2}{4} = 1$  तथा अतिपरवलय  $\frac{x^2}{9} - \frac{y^2}{4} = 1$  की उत्केंद्रताएँ हैं तथा  $(e_1, e_2)$  दीर्घवत्

$15x^2 + 3y^2 = k$  पर स्थित एक बिन्दु है, तो  $k$  का मान है :



**Sol.** 4

$$e_1^2 = 1 - \frac{4}{18} = \frac{7}{9}$$

$$= e_1 = \frac{\sqrt{7}}{3} \dots (1)$$

$$= e_2 = \sqrt{1 + \frac{4}{9}} = \frac{\sqrt{13}}{3} \dots (2)$$

$$\Rightarrow 15(e_1)^2 + 3(e_2)^2 = k$$

$$\Rightarrow 15\left(\frac{7}{9}\right) + 3\left(\frac{13}{9}\right) = k$$

$$\Rightarrow k=16$$

- 19.** In a box, there are 20 cards , out of which 10 are labelled as A and the remaining 10 are labelled as B. Cards are drawn at random one after the other and with replacement, till a second A-card is obtained. The probability that the second A-card appears before the third B-card is :

एक बक्से में 20 कार्ड हैं जिनमें से 10 पर A अंकित किया गया है तथा शेष 10 पर B अंकित किया गया है। बक्से में से यद्यच्छया एक के बाद एक (प्रतिस्थापना सहित) कार्ड तब तक निकाले गए जब तक कि दूसरा A से अंकित कार्ड न आ जाए। दूसरे A से अंकित कार्ड के तीसरे B से अंकित कार्ड से पहले आने की प्रायिकता है :

- $$(1) \frac{15}{16} \quad (2) \frac{11}{16} \quad (3) \frac{9}{16} \quad (4) \frac{13}{16}$$

Sol. 2

$$R_{eq} = P(A \cap A) + P(A \cap B \cap A) + P(B \cap A \cap A) + P(B \cap B \cap A \cap A) + P(A \cap B \cap B \cap A) + P(B \cap A \cap B \cap A)$$

$$= \frac{1}{4} + \frac{1}{8} + \frac{1}{8} + \frac{1}{16} \times 3 = \frac{11}{16}$$

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20. If for some  $\alpha$  and  $\beta$  in  $R$ , the intersection of the following three planes

$$x + 4y - 2z = 1$$

$$x + 7y - 5z = \beta$$

$$x + 5y + \alpha z = 5$$

is a line in  $R^3$ , then  $\alpha + \beta$  is equal to :

यदि  $R$  में किन्हीं  $\alpha$  तथा  $\beta$  के लिए, निम्न तीन समतलों

$$x + 4y - 2z = 1$$

$$x + 7y - 5z = \beta$$

$$x + 5y + \alpha z = 5$$

का प्रतिच्छेदन,  $R^3$  में एक रेखा है, तो  $\alpha + \beta$  का मान है :

(1) 0

(2) -10

(3) 10

(4) 2

**Sol.**

**3**

$$\Delta = 0$$

$$\begin{vmatrix} 1 & 4 & -2 \\ 1 & 7 & -5 \\ 1 & 5 & \alpha \end{vmatrix} = 0$$

$$1(7\alpha + 25) - 4(\alpha + 5) - 2(5 - 7) = 0$$

$$7\alpha + 25 - 4\alpha - 20 + 4 = 0$$

$$3\alpha + 9 = 0$$

$$\alpha = -3$$

also,

$$\Delta = \begin{vmatrix} 1 & 4 & 1 \\ 1 & 4 & \beta \\ 1 & 5 & 5 \end{vmatrix} = 0$$

$$= 1(35 - 5\beta) - 4(5 - \beta) + (-2) = 0$$

$$= 13 - \beta = 0$$

$$\beta = 13$$

21. If the vectors,  $\vec{p} = (a+1)\hat{i} + a\hat{j} + a\hat{k}$ ,  $\vec{q} = a\hat{i} + (a+1)\hat{j} + a\hat{k}$  and  $\vec{r} = a\hat{i} + a\hat{j} + (a+1)\hat{k}$  ( $a \in R$ ) are coplanar and  $3(\vec{p} \cdot \vec{q})^2 - \lambda |\vec{r} \times \vec{q}|^2 = 0$ , then the value of  $\lambda$  is

यदि सदिश  $\vec{p} = (a+1)\hat{i} + a\hat{j} + a\hat{k}$ ,  $\vec{q} = a\hat{i} + (a+1)\hat{j} + a\hat{k}$  तथा  $\vec{r} = a\hat{i} + a\hat{j} + (a+1)\hat{k}$  ( $a \in R$ ) सहतलीय हैं तथा

$$3(\vec{p} \cdot \vec{q})^2 - \lambda |\vec{r} \times \vec{q}|^2 = 0$$

है, तो  $\lambda$  का मान है.....

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**उत्थान**

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99 percentile and above  
in JEE Main (Jan-2020)

Fees - ₹ 11000  
score 160-200

Fees - ₹ 5500  
score 200-240

Fees - ₹ 0  
score above 240

**Sol. 1**

$$[\vec{p} \vec{q} \vec{r}] = \begin{vmatrix} a+1 & a & a \\ a & a+1 & a \\ a & a & a+1 \end{vmatrix} = 0 \Rightarrow \begin{vmatrix} 1 & -1 & 0 \\ a & a+1 & a \\ 0 & -1 & 1 \end{vmatrix} = 0$$

$$1(a+1+a) + 1(a) = 0 \Rightarrow 3a + 1 = 0 \Rightarrow a = -1/3$$

$$\vec{p} = \frac{2}{3}, -\frac{1}{3}, -\frac{1}{3}; \vec{q} = \frac{-1}{3}, \frac{2}{3}, -\frac{1}{3}; \vec{r} = \frac{-1}{3}, -\frac{1}{3}, \frac{2}{3}$$

$$\vec{p} \cdot \vec{q} = -\frac{2}{9} - \frac{2}{9} + \frac{1}{9} = -\frac{4}{9} + \frac{1}{9} = -\frac{1}{3} \Rightarrow \vec{r} \times \vec{q} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ -\frac{1}{3} & \frac{2}{3} & -\frac{1}{3} \\ -\frac{1}{3} & -\frac{1}{3} & \frac{2}{3} \end{vmatrix}$$

$$= \left( \frac{1}{3}, \frac{1}{3}, \frac{1}{3} \right)$$

$$= 3 \times \frac{1}{9} - \lambda \left( \sqrt{\frac{3}{9}} \right)^2 = 0$$

$$\Rightarrow \lambda = 1$$

- 22.** The coefficient of  $x^4$  in the expansion of  $(1+x+x^2)^{10}$  is  
 $(1+x+x^2)^{10}$  के प्रसार में  $x^4$  का गुणाक है .....

**Sol. 615**

$$= \frac{10!}{p!q!r!} (1)^p (x)^q (x^2)^r$$

$$= q+2r=4, p+q+r=10$$

p	q	R
8	0	2
6	4	0
7	2	1

$$= \frac{10!}{8!2!} + \frac{10!}{6!4!} + \frac{10!}{7!2!}$$

$$= 45 + 210 + 360 = 615$$

- 23.** If for  $x \geq 0, y = y(x)$  is the solution of the differential equation,

$$(x+1)dy = ((x+1)^2 + y - 3)dx, y(2) = 0, \text{ then } y(3) \text{ is equal to.....}$$

यदि  $x \geq 0$  के लिए  $y = y(x)$ , अवकल समीकरण  $(x+1)dy = ((x+1)^2 + y - 3)dx, y(2) = 0$ , का हल है, तो  $y(3)$  का मान है .....

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**Sol. 3**

$$(x+1)dy = [(x+1)^2 + (y-3)]dx$$

$$\frac{dy}{dx} - \frac{y}{x+1} = x+1 - \frac{3}{x+1}$$

$$\Rightarrow I.F. = e^{-\int \frac{dx}{x+1}} = \frac{1}{x+1}$$

$$\Rightarrow \frac{y}{x+1} = \int \frac{x^2 + 2x - 2}{(x+1)^2} dx$$

$$\Rightarrow \frac{y}{x+1} = x + \frac{3}{x+1} + C$$

Equation passes through (2,0) then, C = -3

$$= \frac{y}{x+1} = x + \frac{3}{x+1} - 3$$

Put x = 3 then, y = 3

- 24.** The number of distinct solutions of the equation,  $\log_{\frac{1}{2}} |\sin x| = 2 - \log_{\frac{1}{2}} |\cos x|$  in the interval  $[0, 2\pi]$  is .....

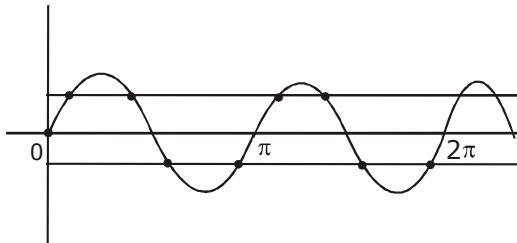
समीकरण  $\log_{\frac{1}{2}} |\sin x| = 2 - \log_{\frac{1}{2}} |\cos x|$  के अंतराल  $[0, 2\pi]$  में मिन्न हलों की संख्या है .....

**Sol. 8**

$$\log_{\frac{1}{2}} |\sin x| = 2 - \log_{\frac{1}{2}} |\cos x|$$

$$= |\sin x||\cos x| = \frac{1}{4}$$

$$= \sin 2x = \pm \frac{1}{2}$$



- 25.** The projection of the line segment joining the points (1, -1, 3) and (2, -4, 11) on the line joining the points (-1, 2, 3) and (3, -2, 10) is .....

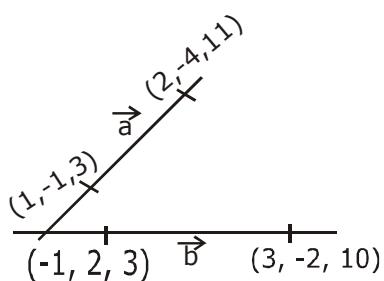
बिन्दुओं (1, -1, 3) तथा (2, -4, 11) को मिलाने वाले रेखाखण्ड का बिन्दुओं (-1, 2, 3) तथा (3, -2, 10) को मिलाने वाली रेखा पर प्रक्षेप है .....

**Sol. 8**

$$\vec{a} = 1, -3, 8$$

$$\vec{b} = 4, -4, 7$$

$$= \frac{\vec{a} \cdot \vec{b}}{|\vec{b}|} = \frac{4 + 12 + 56}{\sqrt{16 + 16 + 49}} = 8$$



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