

(Page # 3)

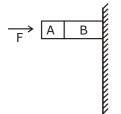
 $\frac{1}{2}\frac{dg}{g} = \frac{1}{400} + \frac{1}{90}$ $\frac{dg}{g} = \left(\frac{490}{400 \times 90}\right) \times 2$ $= \left(\frac{490}{200 \times 90}\right) = 0.20272$ $= dg/g \times 100 \approx 2.72\% \approx 3\%$ $\xrightarrow{F} A B$ Given the figure are two block weight 20 N and 100 N, respectively.

3.

Sol.

Given the figure are two blocks A and B of weight 20 N and 100 N, respectively. These are being pressed against a wall by a force F as shown. If the coefficient of friction between the blocks is 0.1 and between block B and the wall is 0.15, the frictional force applied by the wall on block B is :

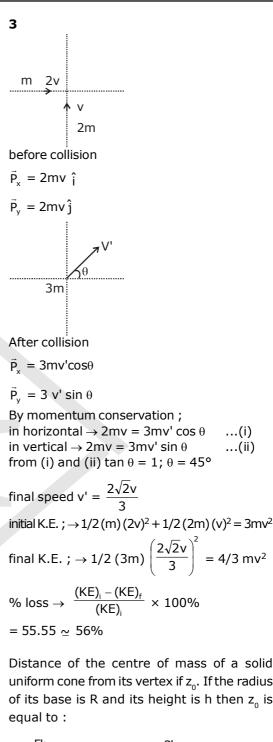
(1) 100 N (3) 120 N (4) 80 N **3**



Assume the system is in equilibrium. Net gravitational force must be balanced by friction force from the wall. Force of friction = 120 N

4. A particle of mass m moving in the x direction with speed 2υ is hit by another particle of mass 2m moving in the y direction with speed υ . if the collision is perfectly inelastic, the percentage loss in the energy during the collision is close to :

(1) 44%	(2) 62%
(3) 56%	(4) 50%

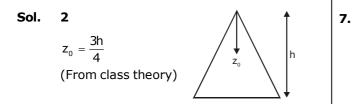


(1) $\frac{5h}{8}$ (2) $\frac{3h}{4}$ (3) $\frac{5h}{8}$ (4) $\frac{3h^2}{8R}$

Rank Booster Test Series [JEE Advanced] 12th & 13th Students Start from 6 April. 2015

5.

Sol.



6. From a solid sphere of mass M and radius R a cube of maximum possible volume is cut. Moment of inertia of cube about an axis passing through its center and perpendicular to one of its faces is :

(1)
$$\frac{MR^2}{32\sqrt{2}\pi}$$
 (2) $\frac{4MR^2}{3\sqrt{3}\pi}$
(3) $\frac{4MR^2}{9\sqrt{3}\pi}$ (4) $\frac{MR^2}{16\sqrt{2}\pi}$

$$I = \frac{Mx^2}{6}$$

edge length : (x)

$$2R = \sqrt{3}x$$

$$x = \frac{2R}{\sqrt{3}}$$

Now, mass of cube :

$$m = \frac{M}{\left(\frac{4}{3}\pi R^3\right)} \left(\frac{2R}{\sqrt{3}}\right)^3$$

$$\left(\frac{3M}{4\pi R^3}\right) \left(\frac{8R^3}{3\sqrt{3}}\right)$$

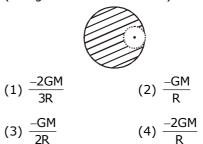
$$m = \frac{2M}{\sqrt{3}\pi}$$

$$I = \frac{1}{3} \left(\frac{2M}{\sqrt{3}\pi}\right) \left[\frac{4R^2}{3}\right]$$
$$= \frac{4MR^2}{3}$$

 $=\overline{9\sqrt{3}\pi}$

JEE MAIN Examination(2015) (Code - A)

From a solid sphere of mass M and radius R, a spherical portion of radius R/2 is removed, as shown in the figure. Taking gravitational potential V = 0 at $r = \infty$, the potential at the centre of the cavityh thus formed is : (G = gravitational constant)



Sol. 2

Solid sphere is of mass M, radius R. Spherical portion removed have radius R/2, therefore its mass is M/8.

Potential at the centre of cavity

=
$$V_{\text{solid sphere}}$$
 + $V_{\text{removed part}}$

$$\frac{-GM}{2R^{3}} \left[3R^{2} - \left(\frac{R}{2}\right)^{2} \right] + \frac{3G(M/8)}{2(R/2)} = \frac{-GM}{R}$$

A pendulum made of a uniform wire of crosssectional area A has time period T. When an additional mass M is added to its bob, the time period changes to T_{M} . If the Young's modulus of the material of the wire is Y then 1/Y is eugal to : (g = gravitational acceleration)

(1)
$$\left[\left(\frac{T_{M}}{T}\right)^{2} - 1\right] \frac{A}{Mg}$$
 (2) $\left[1 - \left(\frac{T}{T_{M}}\right)^{2}\right] \frac{A}{Mg}$
(3) $\left[1 - \left(\frac{T_{M}}{T}\right)^{2}\right] \frac{A}{Mg}$ (4) $\left[\left(\frac{T_{M}}{T}\right)^{2} - 1\right] \frac{Mg}{A}$

Sol.

8.

$$T = 2\pi \sqrt{\frac{\ell}{g}}$$
; $T_M = 2\pi \sqrt{\frac{\ell}{g}}$

9. Consider a spherical shell of radius R at temperature T. The black body radiation inside it can be considered as an ideal gas of photons with internal energy per unit volume

 $u=\frac{U}{V}\propto T^4$ and pressure $p=\frac{1}{3}{\left(\frac{U}{V}\right)}.$ If the

shell now undergoes an adiabatic expansion the relation between T and R is :

(2) $T \propto \frac{1}{R^3}$

(4) $T \propto e^{-3R}$

(1) T
$$\propto e^{-R}$$

(3) $T \propto \frac{1}{R}$ Sol. 3

$$\begin{split} u &= \frac{U}{V} \propto T^{4} \\ P &= \frac{1}{3} \bigg(\frac{U}{V} \bigg) \\ \text{Adiabatic expansion} \\ TV^{\gamma - 1} &= K \\ TV^{\frac{\gamma}{4}} &= C \\ \gamma - 1 &= \frac{\gamma}{4} \\ \frac{3\gamma}{4} &= 1 \\ \gamma &= \frac{4}{3} \\ TV^{\frac{\gamma}{4}} &= C \\ TV^{\frac{1}{3}} &= C \\ TV^{\frac{1}{3}} &= C \\ T \bigg(\frac{4}{3} \pi R^{3} \bigg)^{\frac{1}{3}} &= C \\ T &\propto \frac{1}{R} \end{split}$$

10. A solid body of constant heat capacity 1 J/°C is being heated by keeping it in contact with reservoirs in two ways :

(i) Sequentially keeping in contact with 2 reservoirs such that each reservoir supplies same amount of heat.

(ii) Sequentially keeping in contact with 8 reservoirs such that each reservoirs supplies same amount of heat.

In both the cases body is brought from initial temperature 100°C to final temperature 200°C. Entropy change of the body in the two cases respectively is :

(2) ln2, ln2

(4) 2ln2, 8ln2

(i)
$$\Delta S_1 = \int \frac{dQ}{T} = ms \int_{100}^{150} \frac{dT}{T} + ms \int_{150}^{200} \frac{dT}{T}$$

 $= ln \left(\frac{150}{100}\right) + ln \left(\frac{200}{150}\right)$
 $= ln \left(\frac{3}{2}\right) + ln \frac{4}{3}$
 $\Delta S_1 = ln 2$
(ii) $\Delta S_2 = \int \frac{dQ}{T} = \int_{100}^{112.5} \frac{dQ}{T} + \int_{112.5}^{125} \frac{dQ}{T} + \dots$
 $= ln \left(\frac{112.5}{100}\right) + ln \left(\frac{125}{112.5}\right) + \dots$
 $= ln \left(\frac{9}{8}\right) + ln \left(\frac{10}{9}\right) + ln \left(\frac{16}{15}\right)$
 $= ln \left(\frac{16}{8}\right) = ln 2$

 Consider an ideal gas confined in an isolated closed chamber. As the gas undergoes an adiabatic expansion, the average time of collision between molecules increases as V^q, when V is the volume of the gas. The value

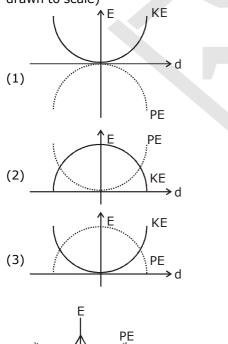
of q is :
$$\left(\gamma = \frac{C_P}{C_V}\right)$$

(1) $\frac{3\gamma + 5}{6}$ (2) $\frac{\gamma - 1}{2}$
(3) $\frac{\gamma + 1}{2}$ (4) $\frac{3\gamma - 5}{6}$

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Sol. 3 mean free path $\lambda = \frac{1}{\sqrt{2}\pi d^2 n}$ $n = \frac{no. \text{ of molecules}}{\text{volume}}$ $v_{\text{avg.}} \propto \sqrt{T}$ $T.V^{\gamma-1} = C$ $t = \frac{\lambda}{v_{\text{avg.}}} \propto \frac{V}{\sqrt{T}}$ $v \rightarrow \text{ is volume}$ $\frac{V}{\sqrt{\frac{C}{V^{r-1}}}} \propto V^{\frac{\gamma+1}{2}}$ $v^q \propto v^{\frac{\gamma+1}{2}}$ $q = \frac{\gamma+1}{2}$

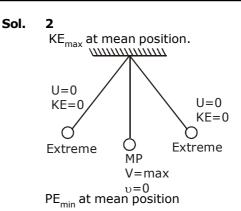
12. For a simple pendulum, a graph is plotted between its kinetic energy (KE) and potential energy (PE) against its displacement d. Which one of the following represents these correctly ? (graphs are schematic and not drawn to scale)



KE

(4)

JEE MAIN Examination(2015) (Code - A)



13. A train is moving on a straight track with speed 20 ms⁻¹. It is blowing its whistle at the frequency of 1000 Hz. The percentage change in the frequency heard by a person standing near the track as the train passes him is (speed of sound = 320 ms^{-1}) close to : (1) 18% (2) 12%

(4) 24%

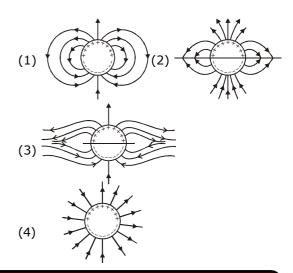
$$f_1 = 1000 \left(\frac{320}{300 - 20}\right) = 1066 \text{ Hz}$$

$$f_2 = 1000 \left(\frac{320}{300 + 20}\right) = 941 \text{ Hz}$$

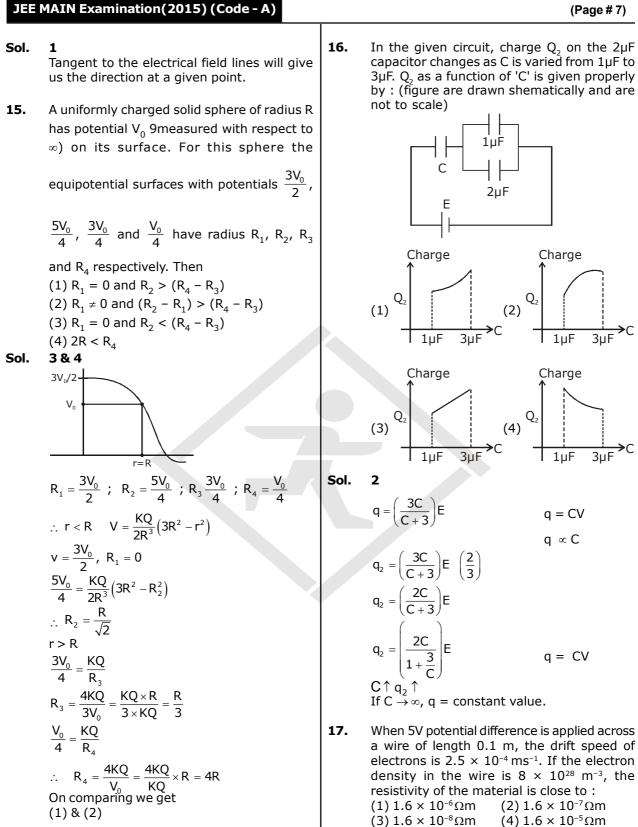
∴ Change is ~ 12%

14. A long cylindrical shell carries positive surface charge σ in the upper half and negative surface charge $-\sigma$ in the lower half. The electric field lines around the cylinder will look like figure given in:

(figures are schematic and not drawn to scale)

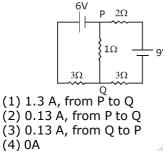


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Sol. 4 $i = neAV_d$ $\Rightarrow \frac{V}{R} = neAV_d$ { $R = \frac{\rho I}{A}$ } $\Rightarrow \frac{V \times A}{\rho \ell} = neAV_d$ $\Rightarrow \frac{5}{\rho \times 0.1} = 8 \times 10^{28} \times 1.6 \times 10^{-19} \times 2.5 \times 10^{-4}$ $\Rightarrow \rho = 1.56 \times 10^{-5} \Omega m$ $\Rightarrow \rho \simeq 1.6 \times 10^{-5} \Omega m$

18. In the circuit shown, the current in the 1Ω resistor is :



Sol.

19. Two coaxial solenoids of different radii carry current I in the same direction. Let \vec{F}_1 be the magnetic force on the inner solenoid due to the outer one and \vec{F}_2 be the magnetic force on the outer solenoid due to the inner one. Then:

(1)
$$\vec{F}_1 = \vec{F}_2 = 0$$

(2)
$$\vec{F}_1$$
 is radially outwards and $\vec{F}_2 = 0$

- (3) $\vec{F}_{_1}$ is radially inwards and $\vec{F}_{_2}$ = 0
- (4) $\vec{F}_{_1}$ is radially inwards and $\vec{F}_{_2}$ is radially outwards

Cross-sectional view

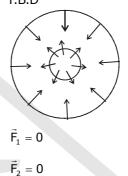


(Both solenoids are taken to be ideal in nature.)

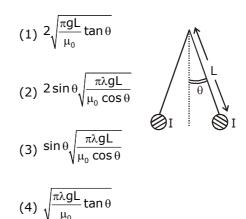
Both wires will attract each other, but net force on each wire will be zero.

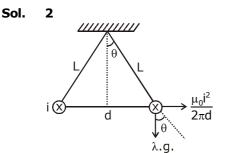
Concept:

Two current carrying elements attract each other if direction of current is same. F.B.D



20. Two long current carrying thin wires, both with current I, are held by insulating threads of length L and are in equilibrium as shown in the figure, with threads making an angle 'θ' with the vertical. If wires have mass λ per unit length then the value of I is : (g = gravitational acceleration)





forces per unit length are taken

$$\tan \theta = \frac{\mu_0 i^2}{2\pi d}$$

$$i^2 = \frac{\lambda g \sin \theta}{\mu_0 \cos \theta} (2\pi) d \qquad [d = 2L \sin \theta]$$

$$i = 2 \sin \theta \sqrt{\frac{\lambda g \pi L}{\mu_0 \cos \theta}}$$

21. A rectangular loop of sides 10 cm and 5 cm carrying a current I of 12 A is placed in different orientations as shown in the figures below ;

If there is a uniform magnetic field of 0.3 T in the positive z direction, in which orientations the loop would be in (i) stable equilibrium and (ii) unstable equilibrium ? (1) (a) and (b), respectively

- (2) (b) and (c), respectively (3) (b) and (d), respectively
- (4) (a) and (c), respectively

Sol.

For equilibrium $\vec{\tau} = 0$

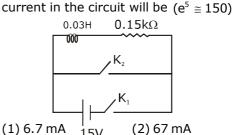
$$\vec{\tau} = MB \sin \theta \hat{n}$$

If, sin
$$\theta = 0$$
; $\tau = 0$

If angle between \vec{M} and \vec{B} is zero, then stable equilibrium

If angle between $\vec{\mathsf{M}}$ and $\vec{\mathsf{B}}$ is $\pi,$ then unstable equilibrium

22. An inductor (L = 0.03H) and a resistor (R = 0.15 k Ω) are connected in series to a battery of 15V EMF in a circuit shown below. The key K₁ has been kept closed for a long time. Then at t = 0, K₁ is opened and key K₂ is closed simultaneously. At t = 1 ms, the



(1) 6.7 mA ¹_{15V} (2) 67 mA (3) 100 mA (4) 0.67 mA **4**

According to given conditions:

$$i_{0} = \frac{V}{R}$$

$$= \frac{15}{0.15 \times 10^{3}}$$

$$= 0.1A$$

$$i = i_{0} e^{-\frac{Rt}{L}}$$

$$= 0.1 \times e^{-\frac{0.15 \times 10^{3} \times 10^{-3}}{0.03}}$$

$$= 0.1 \times e^{-5} = \frac{0.1}{150} = 0.67 \text{ mA}$$

A red LED emits light at 0.1 watt uniformly around it. The amplitude of the electric field of the light at a distance of 1 m from the diode is :
(1) 5.48 V/m
(2) 2.45 V/m

(4) 7.75 V/m

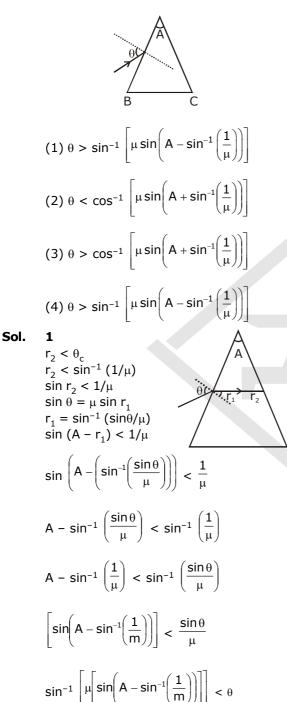
Sol.

Sol.

Intensity
$$= \frac{P}{A} = \frac{1}{2} \epsilon_0 E^2 C$$

 $\Rightarrow \frac{P}{4\pi R^2} = \frac{1}{2} \times \epsilon_0 E^2 C \Rightarrow E = \sqrt{\frac{2P}{4\pi \epsilon_0 R^2 C}}$
 $\Rightarrow E = \sqrt{\frac{2 \times 0.1 \times 9 \times 10^9}{1 \times 1 \times 3 \times 10^8}}$
 $\Rightarrow E = \sqrt{\frac{1.8 \times 10^9}{3 \times 10^8}} = \sqrt{\frac{18}{3}}$
 $\Rightarrow E = \sqrt{6} = 2.45 \text{ V/m}$

24. Monochromatic light is incident on a glass prism of angle A. If the refractive index of the material of the prism is μ , a ray, incident at an angle θ , on the face AB would get transmitted through the face AC of the prism provided :



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25. On a hot summer night, the refractive index of air is smallest near the ground and increases with height from the ground. When a light beam is directed horizontally, the Huygens' principle leads us to conclude that as it travels, the light beam :

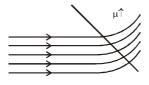
- (1) bends downwards
- (2) goes horizontally without any deflection
- (3) becomes narrower
- (4) bends upwards

4

Bends upwards

(1) 100 µm

(3) 1 µm 2



26. Assuming human pupil to have a radius of 0.25 cm and a comfortable viewing distance of 25 cm, the minimum separation between two objects that human eye can resolve at 500 nm wavelength is : (2) 30 µm

(4) 300 µm

$$y = 1.22 \frac{\lambda D}{d} = \frac{500 \times 10^{-9} \times 25 \times 10^{-2}}{2 \times 0.25 \times 10^{-2}}$$

$$\Rightarrow y = 30 \text{ um}$$

27. An an electron makes a transition from a excited state to the ground state of a hydrogen-like stom/ion :

(1) Its kinetic energy increases but potential energy and total energy decrease.

(2) Kinetic energy and total energy decrease but potential energy increase

(3) Kinetic energy decreases, potential energy increases but total energy remains same (4) Kinetic energy potential energy and total energy decrease

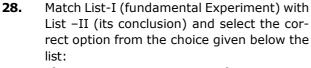
1

$$\mathsf{E}_{\mathsf{Total}} = -13.6 \; \mathsf{eV} \; \frac{\mathsf{Z}^2}{\mathsf{n}^2}$$

$$KE = |E_{Total}|$$

 $PE = 2 E_{total}$

As n decreases, Total energy decreases, potential energy decreases and kinetic energy increases.



(A)

(C)

Sol.

- **List–II** (i) Particle nature of
- (B) Experiment (B) Photo-electric

Franck-Hertz

- Experiment light (ii) Discrete energy
- experiment levels of atom Davison-Germer (iii) Wave nature of Experiment. electron

(iv) Structure of atom

- (1) $A \rightarrow i$; $B \rightarrow iv$; $C \rightarrow iii$ (2) $A \rightarrow iv$; $B \rightarrow iii$; $C \rightarrow ii$
- (2) $A \rightarrow iv$; $B \rightarrow ii$; $C \rightarrow iii$ (3) $A \rightarrow ii$; $B \rightarrow i$; $C \rightarrow iii$
- (3) $A \rightarrow II$; $B \rightarrow I$; $C \rightarrow III$ (4) $A \rightarrow II$; $B \rightarrow IV$; $C \rightarrow III$
- $(4) A \rightarrow II ; B \rightarrow IV$

Photoelectric experiment is linked with particle nature of light

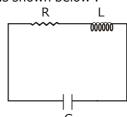
- **29.** A signal of 5 kHZ frequency is amplitude modulated on a carrier wave of frequency 2 MHz. The frequencies of the resultant signal is/are :
 - (1) 2 MHz only
 - (2) 2000 kHz and 1995 kHz
 - (3) 2005 kHz, 2000 kHz and 1995 kHz
 - (4) 2005 kHz and 1995 kHz

Sol.

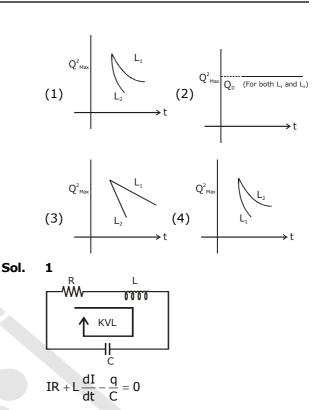
3

Frequencies are F_c , $F_c \pm F_s$

30. An LCR circuit is equivalent to a damped pendulum. In an LCR circuit the capacitor is charged to Q_0 and then connected to the L and R as shown below :



If a student plots graphs of the square of maximum charge (Q_{max}^2) on the capacitor with time (t) for two different values L_1 and L_2 ($L_1 > L_2$) of L then which of the following represents this graph correctly ? (Plots are shematic and not drawn to scale)



$$L\frac{d^2q}{dt^2} = -R\frac{dq}{dt} + \frac{q}{C}$$

comparing with equation of damped oscillation

$$d\frac{d^2y}{dt^2} = -\gamma \frac{dy}{dt} - ky$$

The eqution of amplitude is $y = Ae^{-bt}$

where
$$b = \frac{\gamma}{2m} = \frac{R}{2L}$$

 $\therefore \qquad q_{max} = q_0 e^{-\frac{Rt}{2L}}$
 $\therefore \qquad q_{max}^2 = q_0^2 e^{-\frac{Rt}{L}}$
 $\therefore \qquad time \ constant \ \tau = \frac{R}{L}$
since $L_1 > L_2$
 $\tau_1 < \tau_2$

Hence correct graph is 3.

Alternative solution

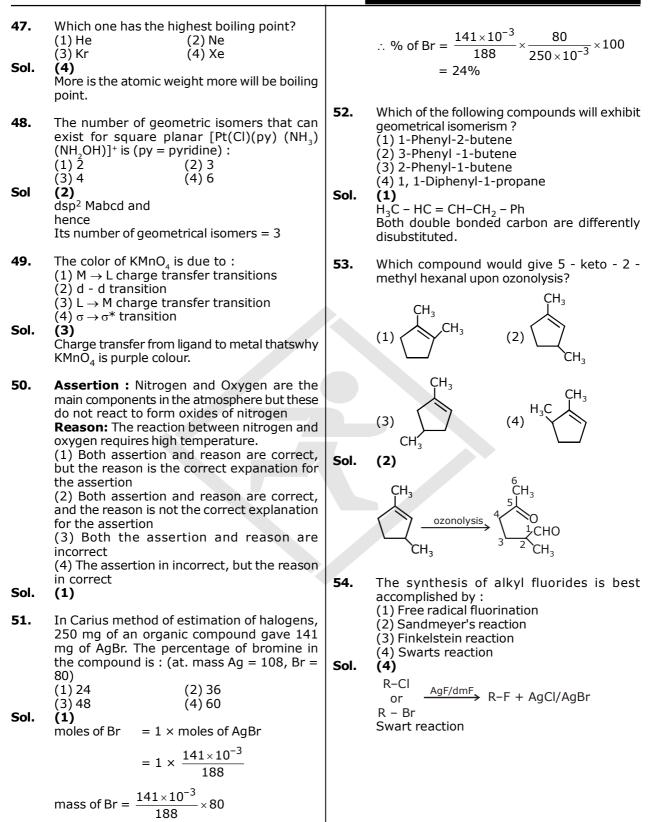
The value of Q_{max} reduces because of energy dissipation in resistor. As the value of inductor increases the time taken for capacity to discharge or charge increases therefore heat dissipation time decreases. Hence correct graph is 3.

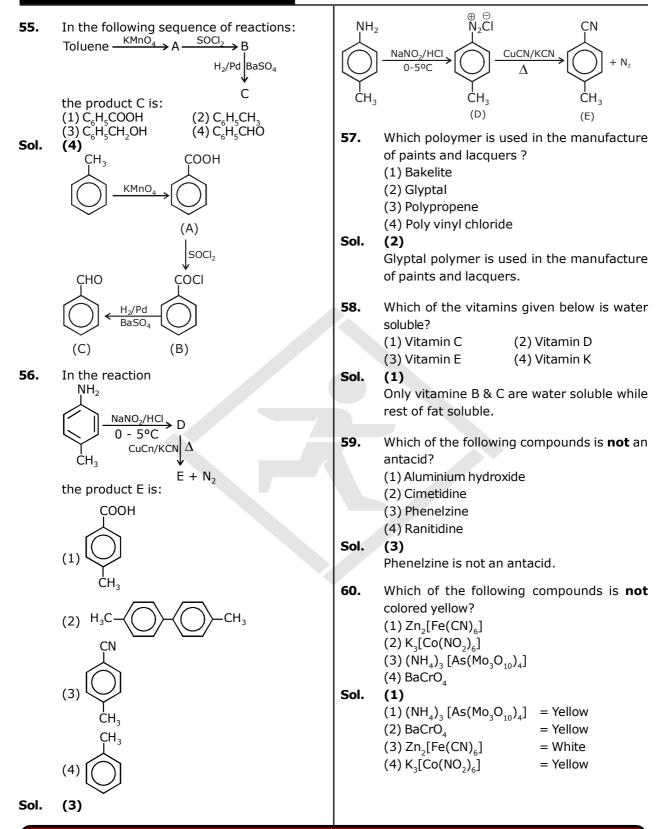
	[CHEMISTRY]				
31.	The moleclar formula of a commercial resin used for exchanging ions in water softening is $C_8H_7SO_3Na$ (Mol. wt. 206). What would be the maximum uptake of Ca^{2+} ions by the resin when expressed in mole per gram resin ? (1) $\frac{1}{103}$ (2) $\frac{1}{206}$	35.	The following reaction is performed at 298 K? $2NO(g) + O_2(g) \rightleftharpoons 2NO_2(g)$ The standard free energy of formation of NO(g) is 86.6 kJ/mol at 298 K. What is the standard free energy of formation of NO ₂ (g) at 298 K? (K _p = 1.6 × 10 ¹²) (1) R(298 ln (1.6 × 10 ¹²) - 86600 (2) 86600 + R(298) ln (1.6 × 10 ¹²)		
Sol.	(3) $\frac{2}{309}$ (4) $\frac{1}{412}$ (4) (4) $2C_8H_7SO_3Na + Ca^{7+} \longrightarrow (C_8H_7SO_3)_2Ca$ $2 \mod 1 \mod 2 \times 206 \text{ gm take } 1 \mod 6 \text{ Ca}^{2+}$ $\therefore 1 \text{ gm takes } \frac{1}{412} \mod 6 \text{ Ca}^{2+}.$	Sol.	(3) 86600 - $\frac{\ln(1.6 \times 10^{12})}{R(298)}$ (4) 0.5[2×86,600-R(298 ln (1.6 × 10 ¹²)] (4) - $\frac{R \times 298 \ln 1.6 \times 10^{12}}{2}$ = $\Delta G^{0}_{r} = 2\Delta G^{0}_{NO_{2}} - 2\Delta G^{0}_{NO}$		
32.	Sodium metal crystallizes in a body centred cubic lattice with a unit cell edge of 4.29 Å. The radius of sodium atom is approximately: (1) 1.86 Å (2) 3.22 Å (3) 5.72 Å (4) 0.93 Å		$\Delta G_{NO_2}^0 = 86.6 \times 10^3 - \frac{298 \text{K} \ln 1.6 \times 10^{12}}{2}$		
Sol. 33.	(1) $\sqrt{3}a = 4r$ $r = \frac{1.732 \times 4.29}{4} = 1.86Å$ Which of the following is the energy of a	36. Sol.	The vapour pressure of acetone at 20° C is 185 torr. When 1.2 g of a non-volatile substance was dissolved in 100 g of acetone at 20° C, its vapour pressure was 183 torr. The molar mass (g mol ⁻¹) of the substance is: (1) 32 (2) 64 (3) 128 (4) 488 (2)		
Sol.	possible excited state of hydrogen? (1) +13.6 eV (2) -6.8 eV (3) -3.4 eV (4) +6.8 eV (3) $-\frac{13.6z^2}{n^2} \Rightarrow$ for hydrogen ; z = 1 13.6		$\frac{P^{0} = 185}{\frac{P^{0} - P}{P} = \frac{n}{N}}$ $\frac{\frac{185 - 183}{183}}{183} = \frac{1.2/M}{100/58}$ $M = 64$		
34.	$-\frac{13.6}{n^2}$ Possible is -13.6, -3.4, -1.5 etc. The intermolecular interation that is dependent on the inverse cube of distance between the molecules is : (1) ion-ion interaction (2) ion-dipole interaction	37.	The standard Gibbs energy change at 300K for the reaction 2A $B \oplus B$ = B + C is 2494.2J. At a given time, the composition of the reaction mixture is $[A] = \frac{1}{2}$, $[B] = 2$ and $[C] = \frac{1}{2}$. The reaction proceeds in the :		
Sol.	 (3) London force (4) hydrogen bond (4) hydrogen bond is dipole-dipole intraction 		[R = 8.314 J/K/mol, e = 2.718] (1) forward direction because Q > K_c (2) reverse direction because Q > K_c (3) forward direction because Q < K_c (4) reverse direction because Q < K_c		

JEE	MAIN Examination(2015) (Code - A)		(Page # 13)
Sol.	(2) $\Delta G^{\circ} \text{ at } 300\text{K} = 2494.2 \text{ J}$ 2A = 10 B + C $\Delta G^{\circ} = -\text{RT} \ln \text{K}$ $-2494.2 = -8.314 \times 300 \ln \text{K}$ K = 10	41. Sol.	The ionic radii (in Å) of N^{3-} , O^{2-} and F^{-} are respectively: (1) 1.36, 1.40 and 1.71 (2) 1.36, 1.71 and 1.40 (3) 1.71, 1.40 and 1.36 (4) 1.71, 1.36 and 1.40 (3) Isoelectronic species. If number of protons are more size will be less.
38.	$Q = \frac{[B][C]}{[A]^2} = \frac{2 \times \frac{1}{2}}{\left(\frac{1}{2}\right)^2} = 4.$ $Q > K_c \Rightarrow \text{reverse direction.}$ Two Faraday of electricity is passed through a solution of CuSO ₄ . The mass of copper deposited at the cathode is :	42.	In the context of the Hall-Heroult process for the extraction of Al, which of the following statements is false ? (1) CO and CO ₂ are produced in this process (2) Al_2O_3 is mixed with CaF ₂ which lowers the melting point of the mixture and brings conductivity
	(at. mass of Cu = 63.5 amu) (1) 0 g (2) 63.5 g (3) 2g (4) 127g	Sol.	(3) AI^{3+} is reduced at the cathode to form AI (4) Na_3A/F_6 serves as the electrolyte (4)
Sol.	(2) $Cu^{2+} + Ze \rightarrow Cu$ 2 mole deposit 1 mole of Cu $2F \Rightarrow 2 \text{ mole} \rightarrow 1 \text{ mole of } Cu \Rightarrow 63.5 \text{ gm}.$	43.	From the following statements regarding H_2O_2 , choose the incorrect statement? (1) It can act only as an oxidizing agent (2) It decomposes on exposure to light (3) It has to be stored in plastic or wax lined glass bottles in dark
39.	Higher order (>3) reactions are rare due to: (1) low probability of simultaneous collision of all the reacting species (2)increase in entropy and activation energy as more molecules are involved (3) shifting of equilibrium towards reactant due to elastic collisions (4)loss of active species on collision	Sol. 44.	(4) It has to be kept away form dust (1) It acts as oxidizing as well as reducing agent. Which one fo the following alkaline earth metal sulphates has its hydration enthalpy greater than its lattice enthalpy? (1) $CaSO_4$ (2) $BeSO_4$ (3) $BaSO_4$ (4) $SrSO_4$
Sol.	 (4)loss of active species on collision (1) molecularity and order > 3 is not possible because of low probability of simultaneous collision of all the reacting species. 	Sol.	(2) BeSO ₄ is only the soluble sulphate because its hydration energy more than its lattice
40.	3 g of activated charcoal was added to 50 mL of acetic acid solution (0.06N) in a flask. After an hour it was filtered and the strength of the filtrate was found to be 0.042N. The amount of acetic acid adsorbed (per gram of charcoal) is :	45. Sol.	energy. rest of all are ppt. Which among the following is the most reactive ? (1) Cl_2 (2) Br_2 (3) I_2 (4) ICl (4) It has some dipole moment value and it is
Sol.	(1) 18 mg (2) 36 mg (3) 42 mg (4) 54 mg (1) CH ₃ COOH (0.06M) 50 ml m. moles = $50 \times 0.06 = 3$ m. moles left = $50 \times 0.042 = 2.1$ m. moles absorbed = 0.9	46.	$ \begin{array}{llllllllllllllllllllllllllllllllllll$
	mass absorbed = $\frac{0.9 \times 10^{-3} \times 60}{3} \times 10^{3}$ = $\frac{54}{3}$ = 18 mg	Sol.	(C) $CuCl_2$ (iii) Contact process (D) V_2O_5 (iv) Deacon's process (1) (A) - (iii), (B) - (ii), (C) - (iv), (D) (i) (2) (A) - (ii), (B) - (i), (C) - (iv), (D) (iii) (3) (A) - (ii), (B) - (ii), (C) - (iv), (D) (i) (4) (A) - (iii), (B) - (i), (C) - (ii), (D) (iv) (2)

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[MATHEMATICS] 61. Let A and B be two sets containing four and $a_n = \alpha_n - \beta_n n \ge 1$ $a_{40}^{-} - 29_{8}^{-} = \alpha^{10} - \beta^{10} - 2\alpha^{8} + 2\beta^{8}$ two elements respectively. Then the number $\stackrel{\circ}{=} \alpha^8 (a^2 - 2) - b^8 (b^2 - 2)$ of subsets of the set $A \times B$, each having at $= \alpha^8(6\alpha) - \beta^8(6\beta)$ (using (1) least three elements is : $= 6\alpha^9 - 6\beta^9$ (2)256(1) 219= 6a₉ (3) 275 (4) 510now Sol. 1 $\frac{a_{10} - 2a_8}{2a_9} = \frac{6a_9}{2a_9} = 3$ $n(A \times B) = 8$ Total subsets = 28 ${}^{8}C_{0} + 8C_{1} + {}^{8}C_{2}$ = 37 122 No. of Req. Subsets = 256 - 37 = 219. If $A = \begin{vmatrix} 2 & 1 & -2 \end{vmatrix}$ 64. is a matrix satisfying the a 2 b 62. A complex number z is the said to be equation $AA^{T} = 9I$, where I is 3 × 3 identity unimodular if |z| = 1. Suppose z_1 and z_2 are matrix, then the ordered pair (a, b) is equal complex number such that $\frac{z_1 - 2z_2}{2 - z_1 \overline{z_2}}$ is to (1)(2, -1)(2)(-2,1)(4)(-2, -1)(3)(2,1)unimodular and z₂ is not unimodular. Sol. 4 Then the point z_1 lies on a : AAT = 9 I(1) straight line parallel to x-axis $\begin{bmatrix} 1 & 2 & 2 \\ 2 & 1 & -2 \\ a & 2 & b \end{bmatrix} \begin{bmatrix} 1 & 2 & a \\ 2 & 1 & 2 \\ 2 & -2 & b \end{bmatrix} = \begin{bmatrix} 9 & 0 & 0 \\ 0 & 9 & 0 \\ 0 & 0 & 9 \end{bmatrix}$ (2) straight line parallel to y-axis (3) circle of radius 2. (4) circle of radius $\sqrt{2}$. Sol. 3 $a + 4 + 2b = 0 \Rightarrow a + 2b = -4$(i) $\left| \frac{z_1 - 2z_2}{2 - z_1 \overline{z_1}} \right| = 1$ $2a + 2 - 2b = 0 \Rightarrow a - b = -1$(ii) From i and ii $3b = -3 \Rightarrow b = -1$ $(z_1 - 2z_2) (\overline{z}_1 - 2\overline{z}_2) = (2 - z_1\overline{z}_2)(2 - \overline{z}_1z_2)$ a = - 2 65. The set of all values of λ for which the system $|z_1|^2 - 2z_1\overline{z}_2 - 2z_2\overline{z}_1 + 4|z_2|^2 = 4 - 2\overline{z}_1z_2 - 2z_1\overline{z}_2$ of linear equations : $2x_1 - 2x_2 + x_3 = \lambda x_1$ $+ |\mathbf{Z}_1|^2 |\mathbf{Z}_2|^2$ $2x_1 - 3x_2 + 2x_3 = \lambda x_2$ $-x_1 + 2x_2 = \lambda x_3$ $|z_1|^2 |z_2|^2 - |z_1|^2 - 4 |z_2|^2 + 4 = 0$ has a non-trivial solution, (1) is an empty set. $(|z_1|^2 - 4)(|z_2|^2 - 1) = 0$ (2) is a singleton. (3) contains two elements. $\Rightarrow |z_1| = 2$ (4) contains more than two elements.. Sol. 3 Let α and β be the roots of equation x^2 – 6x63. $\Delta = (2 - \lambda) (\lambda^2 + 3\lambda - 4) + 2 (-2 \lambda + 2) + 1$ - 2 = 0. If $a_n = \alpha^n - \beta^n$, for $n \ge 1$, then the $(4-3-\lambda)=0$ value of $\frac{a_{10} - 2a_8}{2a_9}$ is equal to : $-\lambda^{3} - \lambda^{2} + 6\lambda + 8 - 3 - \lambda - 8 = 0$ $-\lambda^3 - \lambda^2 + 5\lambda - 3 = 0$ (1) 6(2) - 6 $\lambda^3 + \lambda^2 - 5\lambda + 3 = 0$ (3) 3 (4) - 3 $(\lambda - 1) (\lambda^2 + 2\lambda - 3) = 0$ Sol. 3 $(\lambda - 1) (\lambda + 3) (\lambda - 1) = 0$ $\lambda = 1, 1, -3$ $x^2 - 6x - 2 = 0 \leq_{\beta}^{\alpha} \Rightarrow \alpha^2 - 6\alpha - 2 = 0$ $\beta^2 - 6\beta - 2 = 0$(1)

- 66. The number of integers greater than 6,000that can be formed, using the digits 3, 5, 6, 7 and 8, without repetition, is :
 (1) 216 (2) 192
 (3) 120 (4) 72
- Sol. 2 6/7/8 ---- \downarrow $3 \times {}^{4}C_{3} \times 3! = 72$ ---- = 120Total = 192
- **67.** The sum of coefficients of integral powers of

x in the binomial expansion of $(1 - 2\sqrt{x})^{50}$ is

(1) $\frac{1}{2} \left(3^{50} + 1 \right)$ (2) $\frac{1}{2} \left(3^{50} \right)$ (3) $\frac{1}{2} \left(3^{50} - 1 \right)$ (4) $\frac{1}{2} \left(2^{50} + 1 \right)$

Sol.

 \Rightarrow

for sum of integral power of x put x = 1 in

$$\frac{\left(1 - 2\sqrt{x}\right)^{50} + \left(1 + 2\sqrt{x}\right)^{50}}{2}$$
$$\frac{3^{50} + 1}{2}.$$

68. If m is the A.M. of two distinct real numbers l and n(l, n > 1) and G_1 , G_2 and G_3 are three geometric means between l and n, then

 $\begin{array}{ll} G_1^4 + 2G_2^4 + G_3^4 \mbox{ equals.} \\ (1) 4 \ l^2 mn & (2) 4 \ lm^2 n \\ (3) 4 \ lmn^2 & (4) 4 \ l^2 m^2 n^2 \\ \textbf{7} \end{array}$

- Sol.
- $$\begin{split} m &= \frac{\ell + n}{2} \quad 2m = \ell + \ell r^4 \\ \ell & G_1 \quad G_2 \quad G_3 \quad n \\ \ell & \ell r \quad \ell r^2 \quad \ell r^3 \quad \ell r^4 = n \\ \ell^4 r^4 + 2\ell^4 r^8 + \ell^4 r^{12} \\ &\Rightarrow \ell^4 r^4 (1 + 2r^4 + r^8) \\ &\Rightarrow \ell^4 r^4 (1 + r^4)^2 \\ &\Rightarrow \ell^4 r^4 \left(\frac{2m}{\ell}\right)^2 \end{split}$$

$$\Rightarrow n \cdot \ell^3 \ \frac{4m^2}{\ell^2}$$
$$\Rightarrow 4\ell m^2 n$$

69. The sum of first 9 terms of the series

$$\frac{1^{3}}{1} + \frac{1^{3} + 2^{3}}{1 + 3} + \frac{1^{3} + 2^{3} + 3^{3}}{1 + 3 + 5} + \dots \text{ is :}$$
(1) 71
(2) 96
(3) 142
(4) 192
2

Sol.

$$T_n = \frac{\Sigma n^3}{\Sigma (2n-1)} = \frac{n^2(n+1)^2}{4 \times n^2}$$

$$\Sigma T_{n} = \frac{1}{4} \left(\Sigma n^{2} + 2\Sigma n + \Sigma 1 \right)$$
$$= \frac{1}{4} \left\{ \frac{n(n+1)(2n+1)}{6} + \frac{2n(n+1)}{2} + n \right\}$$
$$= \frac{1}{4} \left\{ \frac{9 \times 10 \times 19}{6} + 90 + 9 \right\}$$

 $(4) \frac{1}{2}$

$$= \frac{1}{4} \{285 + 99\} = 96$$

70.
$$\lim_{x \to 0} \frac{(1 - \cos 2x)(3 + \cos x)}{x \tan 4x}$$
 is equal to
(1) 4 (2) 3

Sol. 3

(3) 2

7

$$\lim_{x\to 0} \frac{(1-\cos 2x)(3+\cos x)}{x\tan 4x}$$

$$\lim_{x \to 0} \frac{(1 - \cos 2x) \cdot (3 + \cos x)}{x \frac{\tan 4x}{4x} \cdot 4x}$$

$$\lim_{x \to 0} \left[\frac{(1 - \cos 2x)}{(2x)^2} \right] \cdot \frac{(3 + \cos x)}{\frac{\tan 4x}{4x}}$$
$$\Rightarrow \quad \frac{1}{2} \cdot (3 + 1) = 2$$

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 $\int k\sqrt{x+1}, \quad 0 \le x \le 3$ 71. If the function g(x) = $\int mx + 2$, $3 < x \le 5$ is differentiable, then the value of k + m is : (2) $\frac{16}{5}$ (1) 2(3) $\frac{10}{3}$ (4) 4Sol. 1 $g(x) = \begin{cases} k\sqrt{x+1} & x \in [0,3] \\ mx+2 & x \in (3,5] \end{cases}$ $g(x) \text{ diff} \Rightarrow g(x) \text{ continuous}$ $g(3^{-}) = g(3^{+})$ *.*.. $k\sqrt{4} = 3m + 2$ 73. \Rightarrow \Rightarrow 2k = 3m + 2(1) Again $g'(3^+) = g'(3^-)$ $m = \left(\frac{k}{2\sqrt{x+1}}\right)_{x=3} = \frac{k}{4}$ Sol. \Rightarrow 4m = k....(2) \Rightarrow from (1) & (2) $2k = 3m + 2 \Rightarrow 8m = 3m + 2$ 5 m = 2 $m = \frac{2}{5}$ $k = 4m = \frac{8}{5}$ & $k + m = \frac{10}{5} = 2$ \Rightarrow 72. The normal to the curve, $x^2 + 2xy - 3y^2 = 0$, at (1, 1) : (1) does not meet the curve again. (2) meets the curve again in the second quadrant. (3) meets the curve again in the third quadrant. (4) meets the curve again in the fourth 74 quadrant. Sol. 4 $x^2 + 2xy - 3y^2 = 0$ diff. w.r.t. x 2x + 2x(y') + 2y - 6yy' = 02 + 2y' + 2 - 6y' = 0

> 4y' = 4y' = 1slope of normal = -1

So equation becomes

 \Rightarrow

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\begin{array}{l} y - 1 = -1 \ (x - 1) \\ x + y = 2 \\ \\ \text{solving it with curve} \\ x^2 + 2xy - 3y^2 = 0 \\ x^2 + 2x(2 - x) - 3(2 - x)^2 = 0 \\ x^2 + 4x - 2x^2 - 3(x^2 - 4x + 4) = 0 \\ -4x^2 + 16x - 12 = 0 \\ x^2 - 4x + 3 = 0 \\ (x - 1) \ (x - 3) = 0 \\ x = 1, 3 \\ \Rightarrow \quad y = 1, -1 \\ \\ \text{thus second point of intersection is (3, -1)} \\ \text{is in 4}^{\text{th}} \ \text{qud.} \\ \\ \text{Let f(x) be a polynomial of degree four having} \end{array}
```

3. Let f(x) be a polynomial of degree four having extreme values at x = 1 and x = 2.

$$\lim_{x \to 0} \left[\frac{1 + \frac{f(x)}{x^2}}{x^2} \right] = 3, \text{ then } f(2) \text{ is equal to } :$$

-8 (2) -4
0 (4) 4

f(x) =

If L

(1)

(3)

$$\lim_{x \to 0} \left[1 + \frac{f(x)}{x^2} \right] = 3$$

 \Rightarrow f(x) must not contain degree 0 & degree 1 term

$$\Rightarrow f(x) = ax^{4} + bx^{3} + cx^{2}$$

now f'(x) = 4ax^{3} + 3bx^{2} + 2cx
f'(1) = 4a + 3b + 2c = 0(1)
f'(2) = 32a + 12b + 4c = 0(2)

and
$$\lim_{x \to 0} \left[1 + \frac{f(x)}{x^2} \right] = 1 + c = 3 \dots (3)$$
$$\Rightarrow c = 2$$

$$(1) \Rightarrow 4a + 3b = -4$$

$$(2) \Rightarrow 32a + 12b = -8$$

$$(1) \Rightarrow 32a + 24b = -32$$

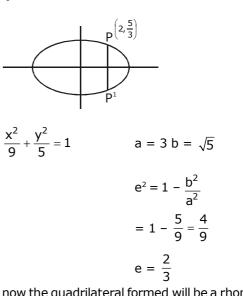
$$(1) \Rightarrow a = \frac{1}{2}$$

4. The integral
$$\int \frac{dx}{x^2(x^4+1)^{3/4}}$$
 equals :
(1) $\left(\frac{x^4+1}{x^4}\right)^{1/4} + c$ (2) $\left(x^4+1\right)^{1/4} + c$
(3) $-\left(x^4+1\right)^{1/4} + c$ (4) $-\left(\frac{x^4+1}{x^4}\right)^{1/4} + c$

Sol. 4

$$\int \frac{dx}{x^{2}(x^{4}+1)^{3/4}} = \int \frac{x^{-5}}{(1+x^{-4})^{3/4}} dx \dots (1)$$
put $1 + x^{-4} = T^{4}$
 $- 4x^{-5} dx = 4T^{3} dT$
 \Rightarrow (1) become
 $-\int \frac{T^{3}dT}{T^{3}} = -T + C$
 $= -(1 + x^{-4})^{1/4} + C$
 $= -\left(\frac{1+x^{4}}{x^{4}}\right)^{1/4} + C$
75. The integral $\int_{2}^{4} \frac{\log x^{2}}{\log x^{2} + \log(36 - 12x + x^{2})} dx$ is
equal to :
(1) 2 (2) 4
(3) 1 (4) 6
Sol. 3
 $I = \int_{2}^{4} \frac{\log x^{2}}{\log x^{2} + \log(x - 6)^{2}} dx \dots (1)$
 $using \int_{a}^{b} f(x) dx = \int_{a}^{b} f(a + b - x) dx$
 $I = \int_{2}^{4} \frac{\log (6-x)^{2}}{\log (6-x)^{2} + \log x^{2}} dx \dots (2)$
(1) + (2) gives
 $2I = \int_{2}^{4} 1 dx = 2$
 $I = 1$
76. The area (in sq. units) of the quadrilateral formed
by the tangents at the end points of the lateral
recta to the ellipse $\frac{x^{2}}{9} + \frac{y^{2}}{5} = 1$, is :
(1) $\frac{27}{4}$ (2) 18

(3) $\frac{27}{2}$ (4) 27



now the quadrilateral formed will be a rhombus

with area = $\frac{2a^2}{e}$

Sol.

4

$$=\frac{2.9}{2}\times 3$$
$$=27$$

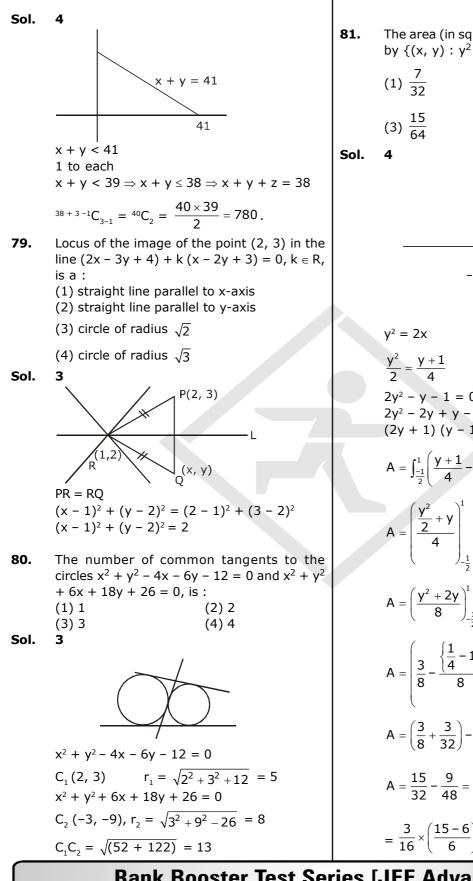
77. Let y(x) be the solution of the differential equation (x log x) $\frac{dy}{dx}$ + y = 2x log x, (x \ge 1). Then y(e) is equal to : (1) e (2) 0(4) 2e (3) 2 Sol. 3

$$\frac{dy}{dx} + \frac{1}{x \log x} \cdot y = 2$$
I.F. = $e^{\int \frac{1}{x \log x}} = e^{\log(\log x)} = \log x$
 $y \cdot \log x = \int 2 \cdot \log x dx$
 $y \log x = 2 (x \log x - x) + c$
 $x = 1 \Rightarrow c = 2$
 $x = e \Rightarrow y = 2(e - e) + 2 = 2$

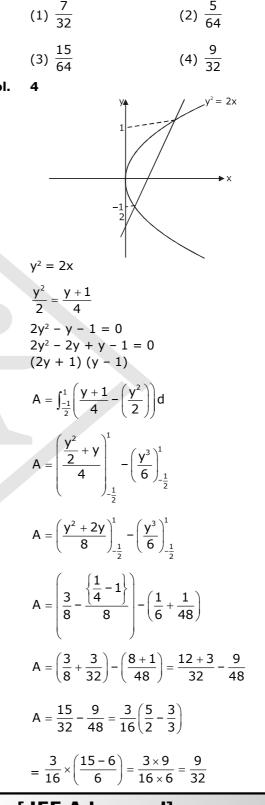
x = e ⇒

78. The number of points, having both coordinates as integers, that lie in the interior of the triangle with vertices (0, 0), (0, 41)and (41, 0), is (1) 901 (2) 861 (3) 820 (4) 780

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81. The area (in sq. units) of the region described by $\{(x, y) : y^2 \le 2x \text{ and } y \ge 4x - 1\}$ is



- 82. Let O be the vertex and Q be any point on Sol. 3 the parabola, $x^2 = 8y$. If the point P divides the line segment OQ internally in the ratio 1 : 3, then the locus of P is (1) $x^2 = y$ (2) $y^2 = x$ (3) $y^2 = 2x$ (4) $x^2 = 2y$ Sol. 4 85. Let P : (h, k) $h = \frac{1 \cdot \alpha + \beta \cdot 0}{4} \Longrightarrow \alpha = 4h$ $\mathsf{k} = \frac{1.\beta + 3.0}{4} \Longrightarrow \beta = 4\mathsf{k}$ \therefore (α , β) on Parabola $\Rightarrow \alpha^2 = 8\beta \Rightarrow (4h^2) = 8.4 \text{ k}$ $16h^2 = 32k$ $x^{2} = 2y$ $(3)\frac{2}{3}$ 83. The distance of the point (1, 0, 2) from the point of intersection of the line $\frac{x-2}{3} = \frac{y+1}{4}$ Sol. $=\frac{z-2}{12}$ and the plane x - y + z = 16, is (1) $2\sqrt{14}$ (2) 8 (3) $3\sqrt{21}$ (4) 13Sol. 4 $P(3\lambda + 2, 4\lambda - 1, 12\lambda + 2)$ $3\lambda + 2 - 4\lambda + 1 + 12\lambda + 2 = 16$ $11\lambda = 11$ $\lambda = 1$ Point of intersection (5, 3, 14) Distance = $\sqrt{4^2 + 3^2 + 12^2}$ 86. $=\sqrt{169}=13$ 84. The equation of the plane containing the line 2x - 5y + z = 3; x + y + 4z = 5, and parallel to the plane, x + 3y + 6z = 1, is (1) 2x + 6y + 12z = 13(2) x + 3y + 6z = -7(3) x + 3y + 6z = 7(4) 2x + 6y + 12z = -13

 - **85.** Let \vec{a}, \vec{b} and \vec{c} be three non- zero vectors such that no two of them are collinear and

$$(\vec{a} \times \vec{b}) \times \vec{c} = \frac{1}{3} |\vec{b}| |\vec{c}| \vec{a}$$
. If θ is the angle

between vectors \vec{b} and \vec{c} , then a value of $sin\theta$ is :

(1)
$$\frac{2\sqrt{2}}{3}$$
 (2) $\frac{-\sqrt{2}}{3}$
(3) $\frac{2}{3}$ (4) $\frac{-2\sqrt{3}}{3}$

$$(\overline{a} \times \overline{b}) \times \overline{c} = \frac{1}{3}bc \ \overline{a}$$
$$(\overline{a}.\overline{c}) \ \overline{b} - (\overline{b}.\overline{c}) \ \overline{a} = \frac{1}{3}bc \ \overline{a} + 0.\overline{b}$$
$$-\overline{b}.\overline{c} = \frac{1}{3}bc, \ \overline{a}.\overline{c} = 0$$
$$-bc \ \cos\theta = \frac{1}{3}bc$$
$$\cos\theta = -\frac{1}{3} \Rightarrow \sin\theta = \frac{2\sqrt{2}}{3}$$

86. If 12 identical balls are to be placed in 3 identical boxes, then the probability that one of the boxes contains exactly 3 balls is :

(1)
$$\frac{55}{3} \left(\frac{2}{3}\right)^{11}$$
 (2) $55 \left(\frac{2}{3}\right)^{10}$
(3) $220 \left(\frac{1}{3}\right)^{12}$ (4) $22 \left(\frac{1}{3}\right)^{11}$

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Sol.

Success (p) = $\frac{1}{3}$ Failure (q) = $\frac{2}{3}$ Acc. to binomial distribution, we have to find, $P(x = 3) = 12_{C_3} \cdot \left(\frac{1}{3}\right)^3 \cdot \left(\frac{2}{3}\right)^9$

 $=\frac{55}{3}\left(\frac{2}{3}\right)^{11}$. 87. The mean of the data set comprising of 16 observations is 16. If one of the observation valued 16 is deleted and three new observations valued 3, 4 and 5 are added to the data, then the mean of the resultant

 $\frac{a_1 + a_2 + a_3 + \dots + a_{15} + 16}{16} = 16 \dots (1)$

$$\frac{a_1 + a_2 + a_3 + \dots + a_{15} + (3 + 4 + 5)}{18} = ??$$

(1)
$$a_1 + a_2 + a_3 + \dots + a_{15} = (16)^2 - 16$$

now

(2)
$$\Rightarrow \frac{(16)^2 - 16 + 12}{18}$$

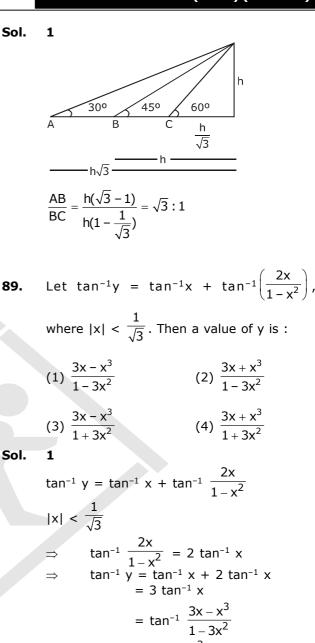
= $\frac{256 - 4}{18} = \frac{252}{18} = 14$
 $\Rightarrow \text{ mean} = 14$

88. If the angles of elevation of the top of a tower from three collinear points A, B and C, on a line leading to the foot of the tower, are 30°, 45° and 60° respectively, then the ratio, AB: BC, is:

(1) $\sqrt{3}:1$	(2) √3 : √2
------------------	-------------

(3) $1:\sqrt{3}$ (4) 2 : 3

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$$\Rightarrow \qquad y = \frac{3x - x^3}{1 - 3x^2}$$

90. The negation of $\sim s v(\sim r \wedge s)$ is equivalent to: (1) s ^ ~ r ′r v ~ s) (2) s ^ (r ^ ~ s) (4) s ^ r

Sol. ~ S V (~ r ^ S)

89.

Sol.

S	r	~ r	~ r ^ S	~ S	~ S V (~ r ^ S)	~ (~ SV(~ r ^ S))
Т	Т	F	F	F	F	Т
Т	F	Т	Т	F	Т	F
F	Т	F	F	Т	Т	F
F	F	Т	F	Т	Т	F