# 

2021

PHYSICS Paper-1 QUESTION WITH SOLUTION

# 32700+ SELECTIONS SINCE 2007



### हो चुकी है ऑफलाइन क्लासरूम की शुरूआत अपने सपने को करो साकार, कोटा कोचिंग के साथ

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Batch Starting from : 6th October 2021

### SECTION - 1

**ANSWER KEY** 

- This section contains **FOUR (04)** questions.
- Each question has **FOUR** options (A), (B), (C) and (D). **ONLY ONE** of these four options is the correct answer.
- For each question, choose the option corresponding to the correct answer.
- Answer to each question will be evaluated according to the following marking scheme:
   Full Marks : +3 If ONLY the correct option is chosen;
   Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered);
   Negative Marks : -1 In all other cases.
- **1.** The smallest division on the main scale of a Vernier calipers is 0.1 cm. Ten divisions of the Vernier scale correspond to nine divisions of the main scale. The figure below on the left shows the reading of this calipers with no gap between its two jaws. The figure on the right shows the reading with a solid sphere held between the jaws. The correct diameter of the sphere is



### Sol. (

In the primary figure with setting up the object. The zero of the two scales have a mismatch , where vernier scales start before main scale so it's a negative zero error &  $6^{th}$  division matches. So zero error (Negative) =  $(10 - 6) \times 0.01 = 0.04$  cm

Now in the second figure, the reading from main scale is 3.1 cm will be added to  $1^{\,\rm st}$  matching division of vernier

So

Reading in 2<sup>nd</sup> figure

(A) 3.07 cm

 $= 3.1 + 1 \times 0.1 = 3.11$  cm

Actual Reading = 3.11 + (Negative zero error)= 3.11 + 0.04

- = 3.15 cm **Ans.**
- 2. An ideal gas undergoes a four step cycle as shown in the P–V diagram below. During this cycle, heat is absorbed by the gas in



### **ANSWER KEY**

### Sol. C

- $\begin{array}{l} 1 \rightarrow \text{Isobaric expansion} \rightarrow \Delta T > 0 \\ 2 \rightarrow \text{Isochoric expansion} \rightarrow \Delta T < 0 \\ 3 \rightarrow \text{Isobaric compression} \rightarrow \Delta T < 0 \\ 4 \rightarrow \text{Isobaric compression} \rightarrow \Delta T > 0 \\ \text{For 2, 4} & \text{for 1,3} \\ Q = nc_v \Delta T & Q = nC_p \Delta T \\ Q > 0 \Rightarrow \Delta T > 0 & Q > 0 \Rightarrow \Delta T > 0 \\ \text{Process 1} & \text{Process 4} \end{array}$
- **3.** An extended object is placed at point O, 10 cm in front of a convex lens  $L_1$  and a concave lens  $L_2$  is placed 10 cm behind it, as shown in the figure. The radii of curvature of all the curved surfaces in both the lenses are 20 cm. The refractive index of both the lenses is 1.5. The total magnification of this lens system is



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4. A heavy nucleus Q of half-life 20 minutes undergoes alpha-decay with probability of 60% and beta-decay with probability of 40%. Initially, the number of Q nuclei is 1000. The number of alpha-decays of Q in the first one hour is (B) 75

(A) 50

(C) 350

(D) 525

**ANSWER KEY** 

#### Sol. D

Given that half life = 20 minutes Number of nucleus of Q at t=0  $N_{o} = 1000$ 

No. of nucleus remaining after t =1hour = N = No $\left(\frac{1}{2}\right)^{n}$ 

$$n = \frac{t}{t_{1/2}} = \frac{60 \text{ minutes}}{20 \text{ minutes}}$$

$$[n = 3]$$
So N<sub>remaining</sub> =  $1000 \cdot \left(\frac{1}{2}\right)^3$ 
(1000)

$$=\left(\frac{1000}{8}\right)$$

So number of total decay in 1 hour

= No - N<sub>remaining</sub>

 $=\left(\frac{7000}{8}\right)$ 

 $\alpha$  decay has probability of 60% So number of  $\alpha$  decay  $\frac{7000}{8} \times \frac{60}{100} = 525 \alpha \text{ decays}$ 

### II<sup>nd</sup> Method

 $1000 \xrightarrow{20\min} 500 \xrightarrow{20\min} 250 \xrightarrow{20\min} 125$ Decay = 1000 - 125 = 875  $\Rightarrow 875 \times 60\% = 525$ 

### Section - 2

- This section contains **THREE (03)** question stems.
- There are **TWO (02)** questions corresponding to each question stem.
- The answer to each question is a **NUMERICAL VALUE.**
- For each question, enter the correct numerical value corresponding to the answer in the designated place using the mouse and the on-screen virtual numeric keypad.
- If the numerical value has more than two decimal places, truncate/round-off the value to **TWO** decimal places.
- Answer to each question will be evaluated according to the following marking scheme: Full Marks : +2 If ONLY the correct numerical value is entered at the designated place; Zero Marks : 0 In all other cases.

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#### **Question Stem for Question Nos. 5 and 6**

#### **Question Stem**

A projectile is thrown from a point O on the ground at an angle 45° from the vertical and with a speed  $5\sqrt{2}$  m/s. The projectile at the highest point of its trajectory splits into two equal parts. One part falls vertically down to the ground, 0.5 s after the splitting. The other part, t seconds after the splitting, falls to the ground at a distance x meters from the point O. The acceleration due to gravity g=10 m/s<sup>2</sup>.

**5.** The value of *t* is \_\_\_\_\_.

### Sol. 0.50

- **6.** The value of *x* is \_\_\_\_\_.
- Sol. 7.50

$$H = H_{max} = \frac{u^2 \sin^2 \theta}{2g} = \frac{(5)^2}{2 \times 10} = 1.25 \text{ m}$$

$$\frac{R}{2} = \frac{u^2 \sin 2\theta}{2g} = 2.5 \text{ m}$$

Given that particle (2m) splits to two equal halves (m,m) Let velocities after split be

$$\mathbf{u}_1 = \mathbf{u}_{\mathbf{x}_1}\mathbf{i} + \mathbf{u}_{\mathbf{y}_1}\mathbf{j}$$

 $u_2^{} = u_{x_2}^{} i + u_{y_2}^{} j$ 

from com

 $mu_1 + mu_2 = 2mu \cos 45^\circ (\hat{i})$ 

$$\Rightarrow u_{x_1} + u_{x_2} = 10 \qquad \dots (1)$$

$$\Rightarrow u_{y_1} + u_{y_2} = 0 \qquad \dots (2)$$

Given that paricle (1) falls vertically down in



 $0.5 \text{ sec} \Rightarrow u_{x_1} = 0$ 

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Now 
$$\Rightarrow H_{max} = u_{x_1}t + \frac{1}{2}gt^2$$
  
 $\Rightarrow \frac{1.25}{0.5} = u_{y_1} + 5(0.5) \Rightarrow u_{y_1} = 0$   
10  
1.25m  
 $t = \sqrt{\frac{2H}{g}} = \sqrt{\frac{2(1.25)}{10}} = \sqrt{0.25} = 0.5 \text{ sec}$   
 $x = 2.5 + R = 2.5 + u \sqrt{\frac{2H}{g}}$   
 $= 2.5 + 10 (0.5) = 7.5 \text{ m}$ 

#### **Question Stem for Question Nos. 7 and 8**

#### **Question Stem**

In the circuit shown below, the switch S is connected to position P for a long time so that the charge on the capacitor becomes  $q_1 \ \mu$ C. Then S is switched to position Q. After a long time, the charge on the capacitor is  $q_2 \ \mu$ C.

**ANSWER KEY** 



**ANSWER KEY** 

## so, $V_A = 2 - i \times 2 = 2 - \frac{2}{3} = \frac{4}{3}$ volt So, $V_A - V_B = \Delta V_{cap} = \frac{4}{3}$ volt Hence, $q_1 = C.\Delta V_{cap} = 1 \times \frac{4}{3} \mu C$ $=\frac{4}{3}\mu C = 1.33\mu C$

$$|q_1| = 1.33$$

8. Sol. The magnitude of  $q_2$  is \_\_\_\_\_. 0.67 When switch is connected from Q for long time



 $|q_2| = 0.67$ 

### Question Stem for Question Nos. 9 and 10

### **Question Stem**

Two point charges -Q and  $+Q/\sqrt{3}$  are placed in the xy-plane at the origin (0, 0) and a point (2, 0), respectively, as shown in the figure. This results in an equipotential circle of radius R and potential V=0 in the xy-plane with its center at (b, 0). All lengths are measured in meters.



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**ANSWER KEY** 

- **9.** The value of R is \_\_\_\_ meter.
- Sol. 1.73



The question says the circle is equipotential and  $V_{circle} = 0$ So,  $V_A = V_B = 0$ 

So, 
$$V_A = \frac{1}{(2-x)} + \frac{1}{\sqrt{3}(x)} = 0$$
  
 $\frac{1}{2-x} = \frac{1}{\sqrt{3}x} \Rightarrow \sqrt{3}x = 2 - x$   
 $x = \frac{2}{(\sqrt{3}+1)} = (\sqrt{3}-1)$  ....(1)  
 $V_B = \frac{-KQ}{(2+y)} + \frac{KQ}{\sqrt{3}(y)} = 0$   
 $\Rightarrow \frac{1}{\sqrt{3}y} = \frac{1}{2+y} \Rightarrow 2 + y = \sqrt{3}y$   
 $y = \frac{2}{(\sqrt{3}-1)} = (\sqrt{3}+1)$   
 $R = \frac{x+y}{2} = \frac{\sqrt{3}-1+\sqrt{3}+1}{2} = \frac{2\sqrt{3}}{2} = \sqrt{3}$   
 $R = \sqrt{3}$ 



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### **ANSWER KEY**

$$\begin{array}{l} \frac{-KQ}{\sqrt{r^2 + y^2}} + \frac{KQ}{\sqrt{3}\sqrt{(2 - x)^2} + y^2}} = 0\\ \frac{KQ}{\sqrt{x^2 + y^2}} = \frac{KQ}{\sqrt{3}\sqrt{4 + x^2 - 4x + y^2}}\\ x^2 + y^2 = 3(x^2 + y^2 - 4x + 4)\\ x^2 + y^2 = 3x^2 + 3y^2 - 12x + 12\\ 2x^2 + 2y^2 - 12x + 12 = 0\\ x^2 + y^2 - 6x + 6 = 0\\ x^2 + y^2 + 2gx + 2fy + c = 0\\ \text{centre (-g, -f) = (3,0), } R = \sqrt{g^2 + f^2 - c}\\ \text{(b,0) = (3,0)} = \sqrt{(3)^2 + 0^2 - 6}\\ \text{b} = 3 \quad R = \sqrt{3} \quad R = \sqrt{3} \end{array}$$

**10.** The value of b is \_\_\_\_ meter.

Sol. 3

So, from A to centre displacement = R A  $\rightarrow$  centre is also equal to b - (2 + x) So, b - (2 + x) = R b - 2 +  $\sqrt{3}$  - 1 =  $\sqrt{3}$ b = 3 b = 3

#### Section – 3

- This section contains SIX (06) questions.
- Each question has FOUR options (A), (B), (C) and (D). ONE OR MORE THAN ONE of these four option(s) is (are) correct answer(s).
- For each question, choose the option(s) corresponding to (all) the correct answer(s).
- Answer to each question will be evaluated according to the following marking scheme:
  - Full Marks: +4 If only (all) the correct option(s) is(are) chosen;Partial Marks: +3 If all the four options are correct but ONLY three options are chosen;Partial Marks: +2 If three or more options are correct but ONLY two options arechosen, both of which are correct;Partial MarksPartial Marks: +1 If two or more options are correct but ONLY one option is chosen and
    - it is a correct option; Zero Marks : 0 If unanswered;
    - Negative Marks : -2 In all other cases.
  - For example, in a question, if (A), (B) and (D) are the ONLY three options corresponding to correct answers, then
    - choosing ONLY (A), (B) and (D) will get +4 marks;
      - choosing ONLY (A) and (B) will get +2 marks;
      - choosing ONLY (A) and (D) will get +2marks;
    - choosing ONLY (B) and (D) will get +2 marks;
      - choosing ONLY (A) will get +1 mark;
      - choosing ONLY (B) will get +1 mark;
    - choosing ONLY (D) will get +1 mark;
    - choosing no option(s) (i.e. the question is unanswered) will get 0 marks and
    - choosing any other option(s) will get -2 marks.

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**11.** A horizontal force F is applied at the center of mass of a cylindrical object of mass m and radius R, perpendicular to its axis as shown in the figure. The coefficient of friction between the object and the ground is  $\mu$ . The center of mass of the object has an acceleration a. The acceleration due to gravity is g. Given that the object rolls without slipping, which of the following statement(s) is(are) correct?

**ANSWER KEY** 



- (A) For the same F, the value of a does not depend on whether the cylinder is solid or hollow
- (B) For a solid cylinder, the maximum possible value of a is  $2\mu g$
- (C) The magnitude of the frictional force on the object due to the ground is always  $\mu$ mg
- (D) For a thin-walled hollow cylinder,  $a = \frac{F}{2m}$

Sol. B,D



Friction has to act backwards to provide  $\alpha$  in acw sense such that  $a = R\alpha$  for pure rolling By NLM (Translational)  $F - f = ma \dots (1)$ N = mgNLM (Rotation)  $\Sigma\tau_0 = I_0\alpha$  $fR = I_0\alpha$  $fR = I_0\alpha$  $fR = \frac{I_0a}{R} (\because a = R\alpha)$  $f = \frac{I_0a}{R^2} \dots (2)$ eq.2 in eq.1 gives  $F - \frac{I_0a}{R^2} = ma$  $\Rightarrow a = \frac{F}{\left(m + \frac{I_0}{R^2}\right)}$ (A) for solid cylinder  $I_0 = \frac{mR^2}{2}$  and for hollow cylinder  $I_0 = mR^2$ 

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 $\Rightarrow a_{\text{solid cylinder}} = \frac{2F}{3m}; \quad a_{\text{hollow cylinder}} = \frac{F}{2m}. \text{ Thus a depends on } I_0 \text{ also. (A) is wrong.}$ (B)  $f = \frac{I_0 a}{R^2} \Rightarrow \text{ as a increases f increases}$  $\Rightarrow a_{\text{max}} = \frac{f_r R^2}{I_0} = \frac{\mu N R^2}{I_0} = \frac{\mu m g R^2}{I_0}$ 

for solid cylinder

 $a_{max} = \frac{\mu mgR^2}{\frac{mR^2}{2}} = 2\mu g$ . Thus (B) is correct.

(C) As long as there is pure rolling the friction is static and self adjusting,  $f = \frac{I_0 a}{R^2}$ . f adjusts its value according to 'a' as long as limiting friction is reached. (C) is wrong. (D) We have already seen that  $a_{\text{hollow cylinder}} = \frac{F}{2m}$ . (D) is right.

**ANSWER KEY** 

The correct options are (B) and (D).

**12.** A wide slab consisting of two media of refractive indices  $n_1$  and  $n_2$  is placed in air as shown in the figure. A ray of light is incident from medium  $n_1$  to  $n_2$  at an angle  $\theta$ , where sin $\theta$  is slightly larger than  $1/n_1$ . Take refractive index of air as 1. Which of the following statement(s) is(are) correct?



- (A) The light ray enters air if  $n_2 = n_1$
- (B) The light ray is finally reflected back into the medium of refractive index  $n_1$  if  $n_2 < n_1$
- (C) The light ray is finally reflected back into the medium of refractive index  $n_1$  if  $n_2 > n_1$

(D) The light ray is reflected back into the medium of refractive index  $n_1$  if  $n_2=1$ **B,C,D** 



(1) If  $n_2 = n_1$ As there is one medium, wave will travel in straight line  $n_2$  air

$$n_1 = n_2 \theta$$

 $n_1 \sin \theta = 1 \times \sin r$ 

Sol.

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as given sin  $\theta > \frac{1}{n_1}$  so sin r will become more than 1 which is not possible.

So, ray will never pass to air.

A is wrong.



**13.** A particle of mass M=0.2 kg is initially at rest in the xy-plane at a point (x=-l,y=-h), where I = 10 m and h=1 m. The particle is accelerated at time t=0 with a constant acceleration a=10 m/s<sup>2</sup> along the positive x-direction. Its angular momentum and torque with respect to the origin, in SI units, are represented by  $\vec{L}$  and  $\vec{\tau}$ , respectively.  $\hat{i}, \hat{j}$  and  $\hat{k}$  are unit vectors along the positive x, y and z-directions, respectively. If  $\hat{k} = \hat{i} \times \hat{j}$  then which of the following statement(s) is(are) correct?

(A) The particle arrives at the point (x=I, y=-h) at time t = 2s

- (B)  $\vec{\tau} = 2\hat{k}$  when the particle passes through the point (x=I, y=-h)
- (C)  $\vec{L} = 4\hat{k}$  when the particle passes through the point (x=I, y=-h)
- (D)  $\vec{\tau} = \hat{k}$  when the particle passes through the point (x=0, y=-h)

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### **ANSWER KEY**

Sol. A,B,C

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### **ANSWER KEY**

 $= -4h(-\hat{k})$ 

 $=4\hat{k}$ 

(D) 
$$\vec{\tau}_{B} = \vec{r}_{B} \times \vec{F}$$

$$= -h\hat{j} \times 2\hat{i}$$

$$= -2h(-\hat{k})$$

 $=2\hat{k}$  (h = 1)

(D) is wrong. Infact  $\vec{\tau}$  remains the same at all points along the line of motion w.r.t. any point on the x –axis.

The correct options are (A), (B) and (C)

- 14. Which of the following statement(s) is(are) correct about the spectrum of hydrogen atom?(A) The ratio of the longest wavelength to the shortest wavelength in Balmer series is 9/5
  - (B) There is an overlap between the wavelength ranges of Balmer and Paschen series
  - (C) The wavelengths of Lyman series are given  $by\left(1+\frac{1}{m^2}\right)\lambda_0$ , where  $\lambda_0$  is the shortest

wavelength of Lyman series and m is an integer (D) The wavelength ranges of Lyman and Balmer series do not overlap

### Sol. À,Ď

For hydrogen atom

$$\frac{1}{\lambda} = R \left[ \frac{1}{n_1^2} - \frac{1}{n_2^2} \right]$$
(A) for Balmer series  
 $n_1 = 2; n_2 = 3, 4, 5, ...$   
 $\frac{1}{\lambda_{\text{longest}}} = R \left[ \frac{1}{2^2} - \frac{1}{3^2} \right] = \frac{5R}{36}$   
 $\frac{1}{\lambda_{\text{shortest}}} = R \left[ \frac{1}{2^2} - \frac{1}{3^2} \right] = \frac{R}{4}$   
 $\Rightarrow \frac{\lambda_{\text{longest}}}{\lambda_{\text{shortest}}} = \frac{36}{5R} \times \frac{R}{4}$   
 $= \frac{9}{5}$   
(A) is correct  
(B) for Paschan series  
 $n_1 = 3, n_2 = 4, 5, ...$   
 $\frac{1}{\lambda_{\text{longest}}} = R \left[ \frac{1}{3^2} - \frac{1}{4^2} \right]$ 

$$=\frac{1}{144}$$

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### **ANSWER KEY**

 $\frac{1}{\lambda_{shortest}} = R \left[ \frac{1}{3^2} - \frac{1}{\infty} \right]$  $= \frac{R}{9}$ 

For Balmer Series

 $\lambda$  ranges from  $\frac{4}{R}$  to  $\frac{36}{5R} = \frac{7.2}{R}$ 

for Paschen Series

 $\lambda$  ranges from  $\frac{9}{R}$  to  $\frac{144}{7R} = \frac{20.57}{R}$ 

Thus there is no overlap. (B) is wrong. In fact Lyman falls is UV region and Balmer falls in Visible region.

(C) In general for Lyman Series,

$$\begin{split} &\frac{1}{\lambda} = R\left(1 - \frac{1}{n_2^2}\right); \ n_2 = 2, 3, 4, \dots \\ &\text{and } \lambda_{\text{shortest}} = \lambda_0 = \frac{1}{R} \\ &\Rightarrow \frac{1}{\lambda} = \frac{1}{\lambda_0} \left(1 - \frac{1}{n_2^2}\right) (\text{let } n_2 \text{ be } m) \\ &\lambda = \lambda_0 \left(1 - \frac{1}{n_2^2}\right)^{-1} \\ &\lambda = \lambda_0 \left(1 + \frac{1}{n_2^2}\right) \\ &\lambda = \lambda_0 \left(1 + \frac{1}{m^2}\right) \end{split}$$

Thus (C) is wrong.

(A) For balmer,  $\lambda$  ranges from  $\frac{4}{R}$  to  $\frac{36}{5R}$ For Lyman,  $\lambda$  ranges from  $\frac{1}{R}$  to  $\frac{4}{3R} = \frac{1.33}{R}$ It's clear that they do not overlap.

**15.** A long straight wire carries a current, I=2 ampere. A semi-circular conducting rod is placed beside it on two conducting parallel rails of negligible resistance. Both the rails are parallel to the wire. The wire, the rod and the rails lie in the same horizontal plane, as shown in the figure. Two ends of the semi-circular rod are at distances 1 cm and 4 cm from the wire. At time t=0, the rod starts moving on the rails with a speed v=3.0 m/s (see the figure).

A resistor R =1.4  $\Omega$  and a capacitor C<sub>0</sub>=5.0  $\mu$ F are connected in series between the rails. At time t=0, C<sub>0</sub> is uncharged. Which of the following statement(s) is(are) correct? [ $\mu_0$ =4 $\pi$ ×10<sup>-7</sup> SI units. Take ln2=0.7]



### **ANSWER KEY**



- (A) Maximum current through R is  $1.2 \times 10^{-6}$  ampere (B) Maximum current through R is  $3.8 \times 10^{-6}$  ampere (C) Maximum charge on capacitor C<sub>0</sub> is  $8.4 \times 10^{-12}$  coulomb (D) Maximum charge on capacitor C<sub>0</sub> is  $2.4 \times 10^{-12}$  coulomb
- A,C

#### Sol.



Consider a small element 'dr' of the semi-ring. The emf is induced due to the component  $\perp$  to V i.e., dx and no emf is induced due to dy. Thus,

$$d\epsilon = BdxV$$

Here, b is the field due to the infinitely long current carrying wire.

$$B = \frac{\mu_0 i}{2\pi x}$$
  

$$\Rightarrow d\epsilon = \frac{\mu_0 i}{2\pi x} \quad V \quad dx$$
  

$$\epsilon = \frac{\mu_0 i v}{2\pi} \int_{1 \text{ cm}}^{4 \text{ cm}} \frac{dx}{x}$$
  

$$= \frac{\mu_0 i v}{2\pi} \times \left[ \ln(4) - \ln(1) \right]$$
  

$$= \frac{2\mu_0 i v \ln(2)}{2\pi}$$

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$$4\pi \times 10^{-7} \times 2 \times 3 \times 0.7$$

 $\pi$  = 16.8 × 10<sup>-7</sup> v.

Now the diagram can be re-written as a circuit as shown.



Since this is a RC charging circuit,

Current is maximum at t= 0, when capacitor can be shorted.

$$i_{max} = \frac{E_0}{R} = \frac{16.8 \times 10^{-7}}{1.4} = 1.2 \times 10^{-6} \text{A}.$$

During steady state i = 0 and charge  $(q_0)$  on the capacitor is maximum. Thus,

$$\begin{aligned} \frac{q_0}{C_0} &= 16.8 \times 10^{-7} \\ q_0 &= 16.8 \times 10^{-7} \times 5 \times 10^{-6} \\ &= 8.4 \times 10^{-12} C \\ (A) \text{ and } (C) \text{ are correct options} \end{aligned}$$

**16.** A cylindrical tube, with its base as shown in the figure, is filled with water. It is moving down with a constant acceleration a along a fixed inclined plane with angle  $\theta$ =45°. P<sub>1</sub> and P<sub>2</sub> are pressures at points 1 and 2, respectively, located at the base of the tube. Let  $\beta$ =( P<sub>1</sub>- P<sub>2</sub>)/( $\rho$ gd), where  $\rho$  is density of water, d is the inner diameter of the tube and g is the acceleration due to gravity. Which of the following statement(s) is(are) correct?



Sol. A,C



#### **SECTION 4**

- This section contains **THREE (03)** questions.
- The answer to each question is a **NON-NEGATIVE INTEGER.**
- For each question, enter the correct integer corresponding to the answer using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.
- Answer to each question will be evaluated <u>according to the following marking scheme:</u> Full Marks : +4 If ONLY the correct integer is entered; Zero Marks : 0 In all other cases.
- **17.** An  $\alpha$ -particle (mass 4 amu) and a singly charged sulfur ion (mass 32 amu) are initially at rest. They are <u>accelerated</u> through a potential V and then allowed to pass into a region of uniform magnetic field which is normal to the velocities of the particles. Within this region, the  $\alpha$ -particle and the sulfur ion move in circular orbits of radii  $r_{\alpha}$  and  $r_{s}$ , respectively. The ratio ( $r_{s}/r_{\alpha}$ ) is \_\_\_\_.



**ANSWER KEY** 

Sol. 4

$$r = \frac{P}{qB} = \frac{\sqrt{2mE}}{qB} = \frac{\sqrt{2mqV}}{qB}$$
$$\Rightarrow r \alpha \sqrt{\frac{m}{q}}$$
$$\Rightarrow \frac{r_s}{r_\alpha} = \sqrt{\frac{m_s}{m_\alpha} \times \frac{q_\alpha}{q_s}}$$
$$= \sqrt{\frac{32}{4} \times \frac{2e}{e}}$$
$$= 4$$

**18.** A thin rod of mass M and length a is free to rotate in horizontal plane about a fixed vertical axis passing through point O. A thin circular disc of mass M and of radius a/4 is pivoted on this rod with its center at a distance a/4 from the free end so that it can rotate freely about its vertical axis, as shown in the figure. Assume that both the rod and the disc have uniform density and they remain horizontal during the motion. An outside stationary observer finds the rod rotating with an angular velocity  $\Omega$  and the disc rotating about its vertical axis with angular velocity  $4\Omega$ .

The total angular momentum of the system about the point O is  $\left(\frac{Ma^2\Omega}{48}\right)$  n.

The value of n is\_\_\_\_\_



#### Sol. 49

$$\begin{split} & \text{For rod} \rightarrow \\ & \text{L}_{\text{rod}} = I_{\text{rod}} \ \omega \\ \Rightarrow \frac{1}{3} \text{Ma}^2 \Omega \\ & \text{For disc} \\ & \text{L}_{\text{disc}} = \text{M} \left( \overrightarrow{r_{\text{cm}}} \times \overrightarrow{v_{\text{cm}}} \right) + I_{\text{disc}}(4\Omega) \\ & \text{V}_{\text{cm}} = \frac{3a}{4} \\ & \text{V}_{\text{cm}} = \frac{3a}{4} \Omega \\ & \Rightarrow \text{L}_{\text{disc}} = \text{M} \left( \frac{9a^2}{16} \Omega \right) + \frac{\text{Ma}^2}{2(16)} \times 4\Omega \\ & \Rightarrow \text{Ma}^2 \Omega \left( \frac{9}{16} + \frac{2}{16} \right) \end{split}$$

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$$\begin{split} &\Rightarrow \frac{11 \text{Ma}^2 \Omega}{16} \\ &\text{L}_{\text{net}} = \text{L}_{\text{rod}} + \text{L}_{\text{disc}} \\ &\Rightarrow \frac{\text{Ma}^2 \Omega}{3} + \frac{11 \text{Ma}^2 \Omega}{16} \\ &\Rightarrow \frac{\text{Ma}^2 \Omega}{48} (16 + 33) \\ &\Rightarrow \frac{\text{Ma}^2 \Omega}{48} (49) \\ &\text{n} = 49 \end{split}$$

**19.** A small object is placed at the center of a large evacuated hollow spherical container. Assume that the container is maintained at 0 K. At time t=0, the temperature of the object is 200 K. The temperature of the object becomes 100 K at t=t<sub>1</sub> and 50 K at t=t<sub>2</sub>. Assume the object and the container to be ideal black bodies. The heat capacity of the object does not depend on temperature. The ratio  $(t_2/t_1)$  is \_\_\_\_.

 $t = t_1$  $t = t_2$ 

#### Sol. 9

Using Stephan Boltzmann Law P =  $\sigma A (T^4 - O^4)$ P =  $\sigma AT^4$   $\frac{dQ}{dt} = \sigma AT^4$   $\Rightarrow -mc \frac{dT}{dt} = \sigma AT^4$   $\Rightarrow \int_{200}^{T} \frac{dT}{T^4} = \int_{0}^{t} -k dt$   $\Rightarrow \left[\frac{1}{3T^3}\right]_{200}^{T} = k(t - 0)$   $\Rightarrow \frac{1}{3} \left[\frac{1}{T^3} - \frac{1}{(200)^3}\right] = k t$   $\Rightarrow If T = 100$  T = 50  $\frac{t_2}{t_1} \frac{\frac{1}{50^3} - \frac{1}{200^3}}{\frac{1}{100^3} - \frac{1}{200^3}} = \frac{1 - \frac{1}{64}}{\frac{1}{8} - \frac{1}{64}}$  $\frac{t_2}{t_1} = \frac{\frac{63}{64}}{\frac{7}{64}} = 9$ 

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